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# ADVANCED BAYESIAN NETWORK MODELLING

## *Outline of the talk*

- ▶ Heuristic search
- ▶ MCMC over structures
  
- ▶ *Other advanced methods/features:*
  - ▶ *Random effect - Clustering*
  - ▶ *Scoring system*
  - ▶ *Tunable parameter prior*
  - ▶ *Structural prior*
  - ▶ *Data separation*
  - ▶ *Covariate adjustment*
  - ▶ *Likelihood contribution*

Find maximum a posteriori score

✓ Exact search

▶ Heuristic search

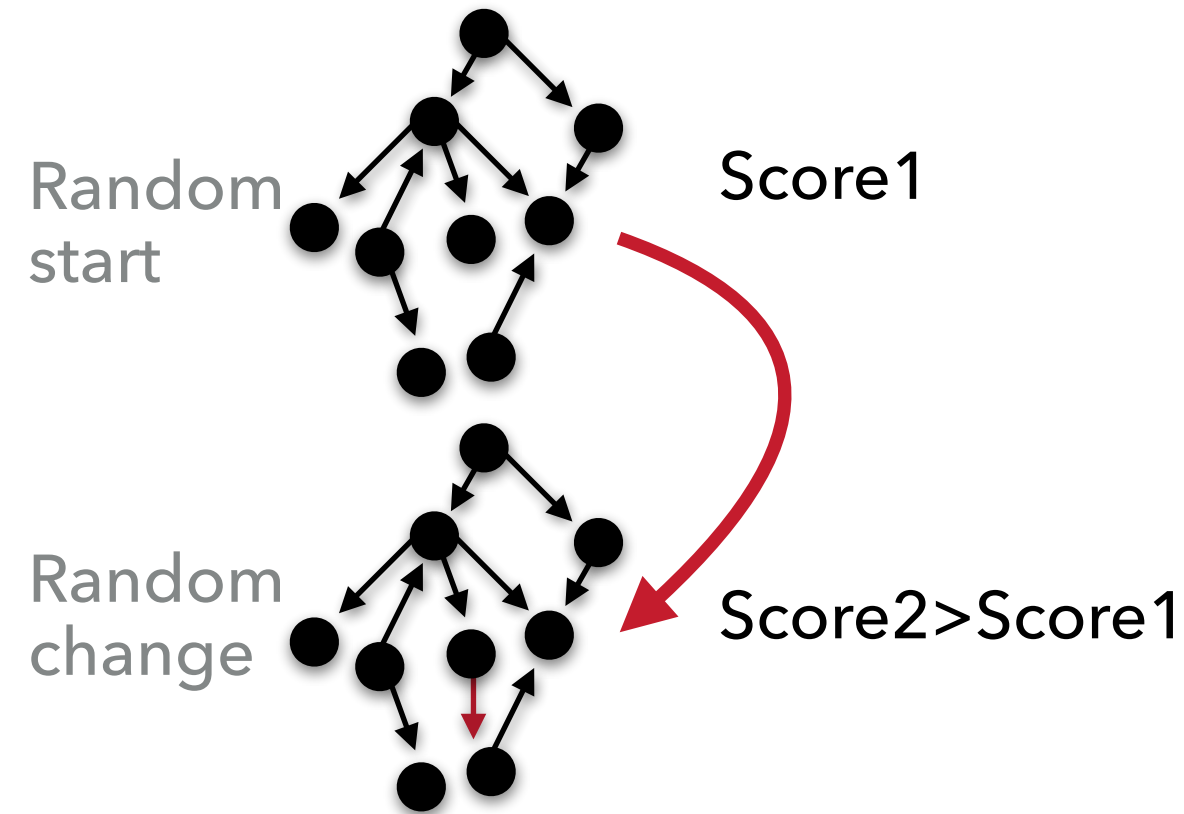
▶ MCMC over structures

# HEURISTIC SEARCH

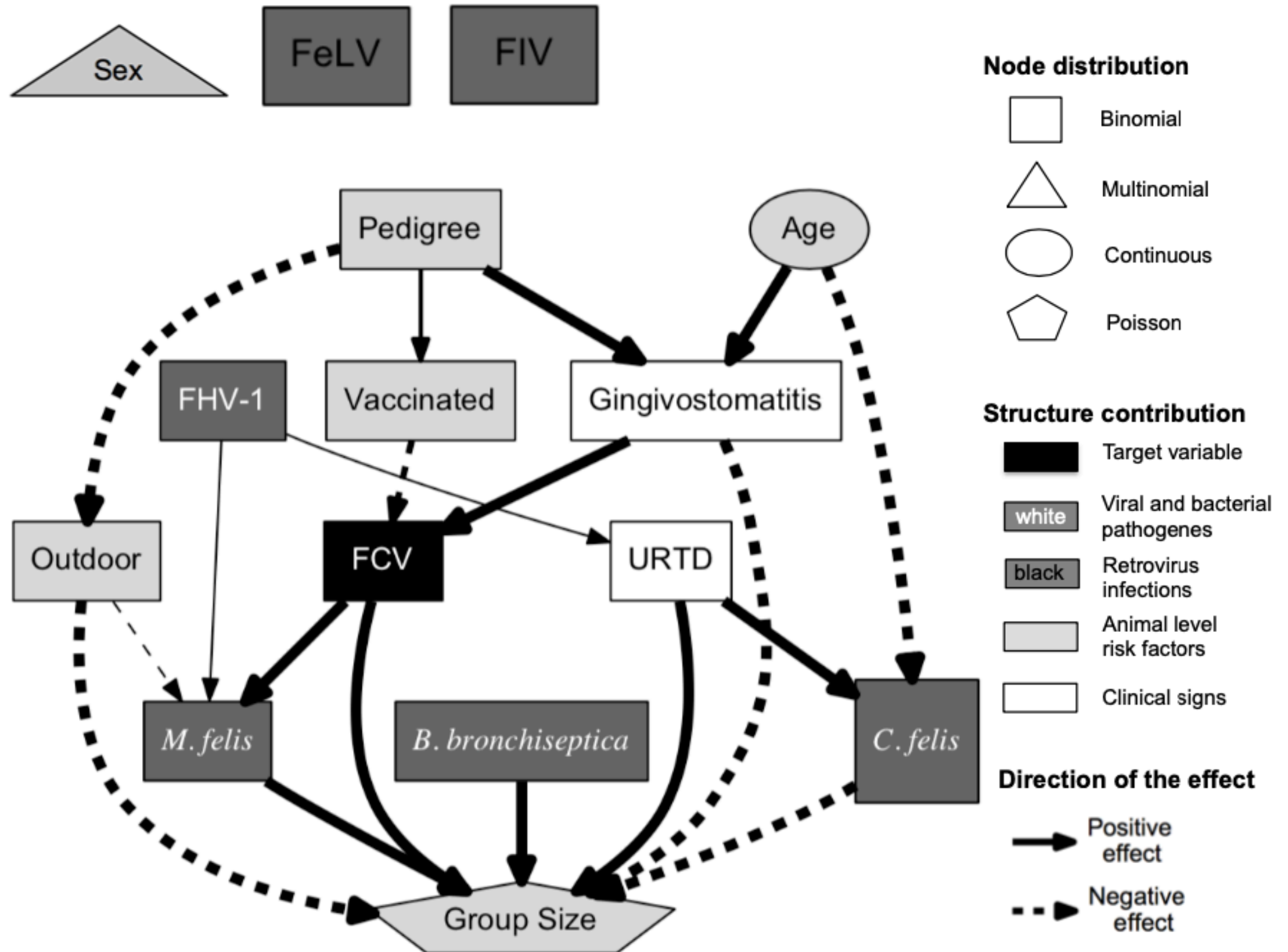
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## *Heuristic search: Greedy Hill-Climbing*

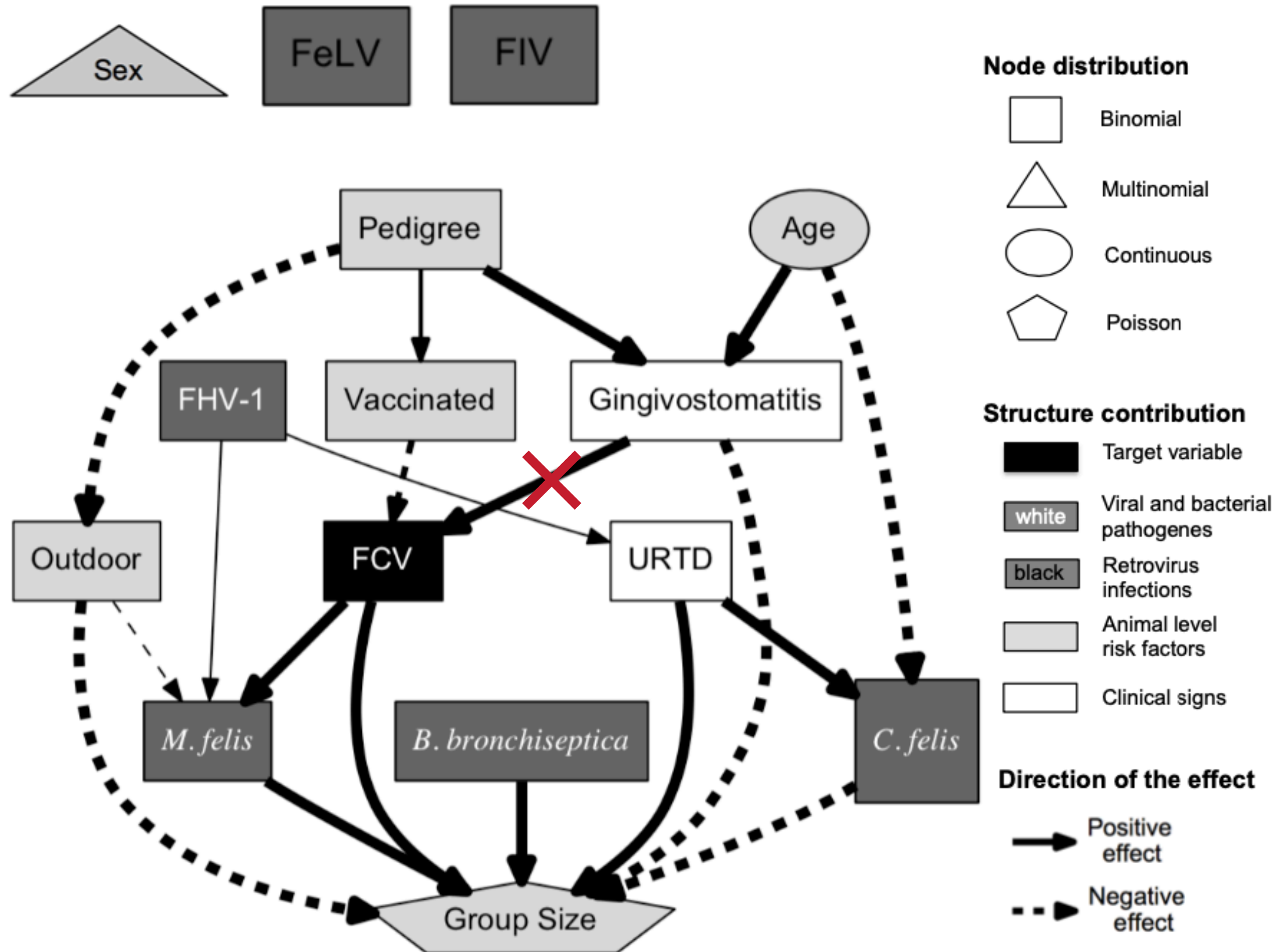
- ▶ Simplest heuristic local search
  - ▶ Start with a given network
    - ▶ empty network
    - ▶ best tree
    - ▶ a random network
  - ▶ At each iteration
    - ▶ Evaluate all possible changes
    - ▶ Apply change that leads to best improvement in score
    - ▶ Reiterate
  - ▶ Stop when no modification improves score
- ▶ *Pitfalls:*
  - ▶ Local Maxima
  - ▶ Plateaus
- ▶ *Solution:*
  - ▶ Tabu
  - ▶ Random restart
  - ▶ Simulated annealing



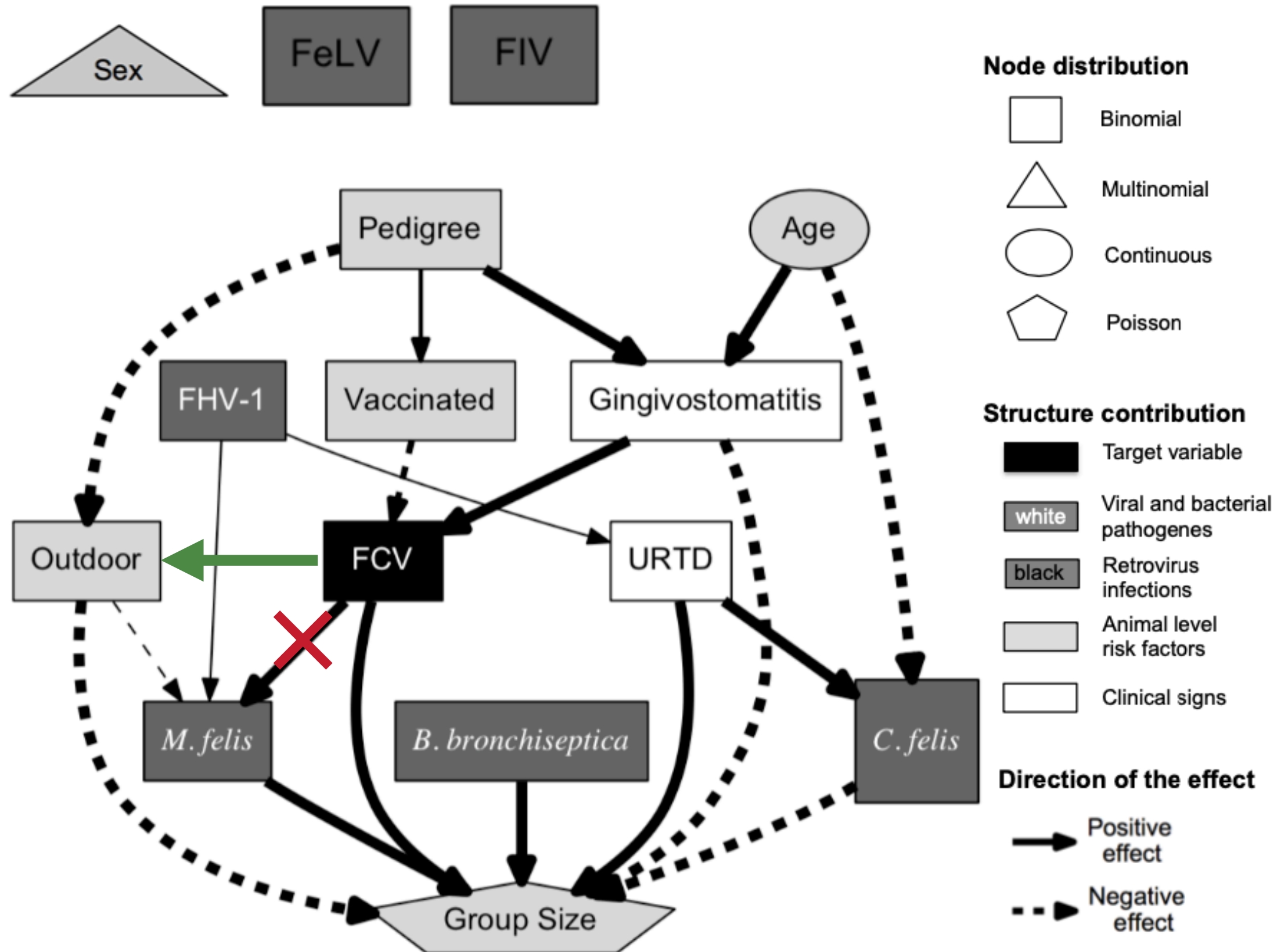
# BAYESIAN NETWORK OF THE “CAT FLU”



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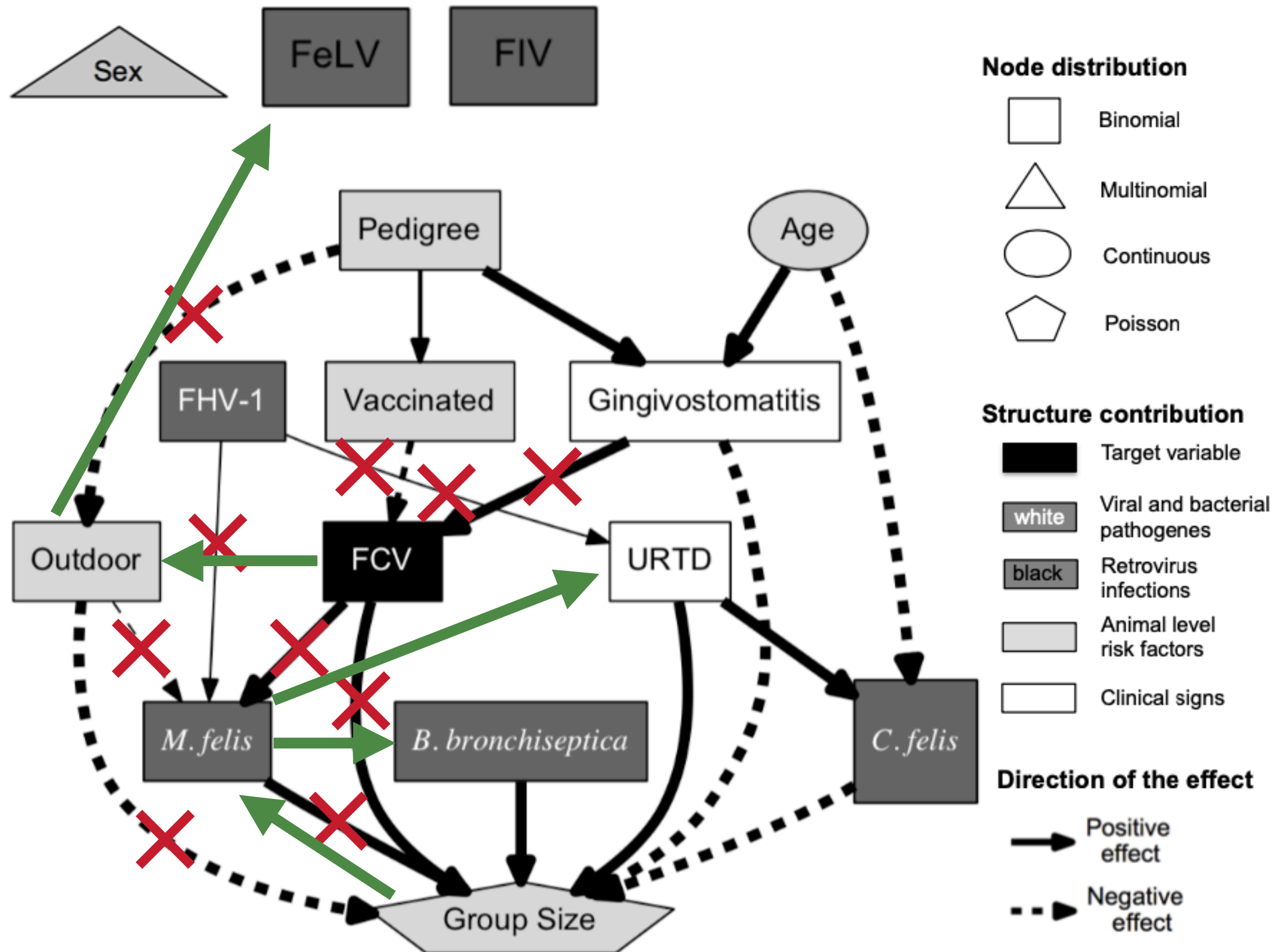


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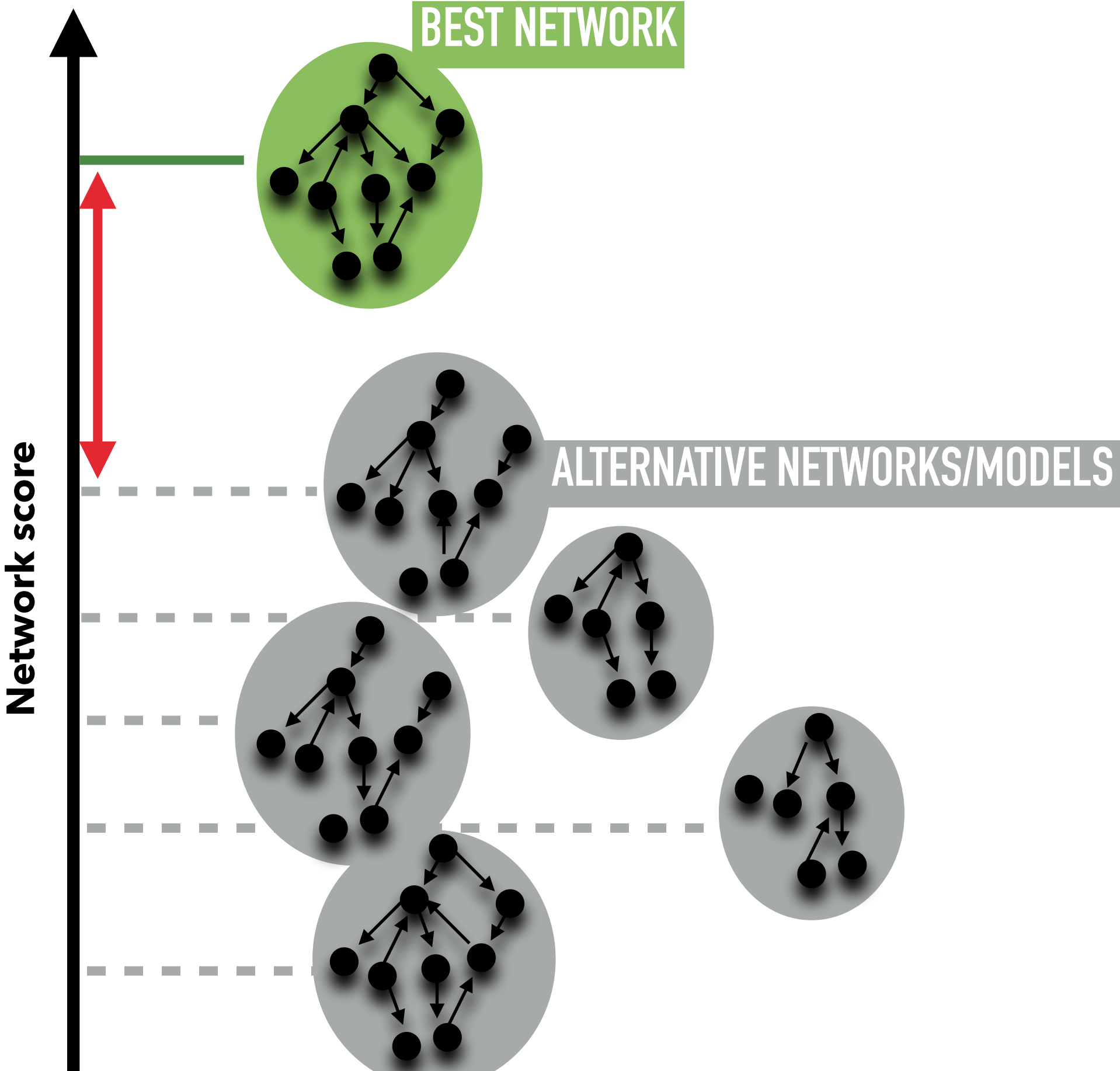




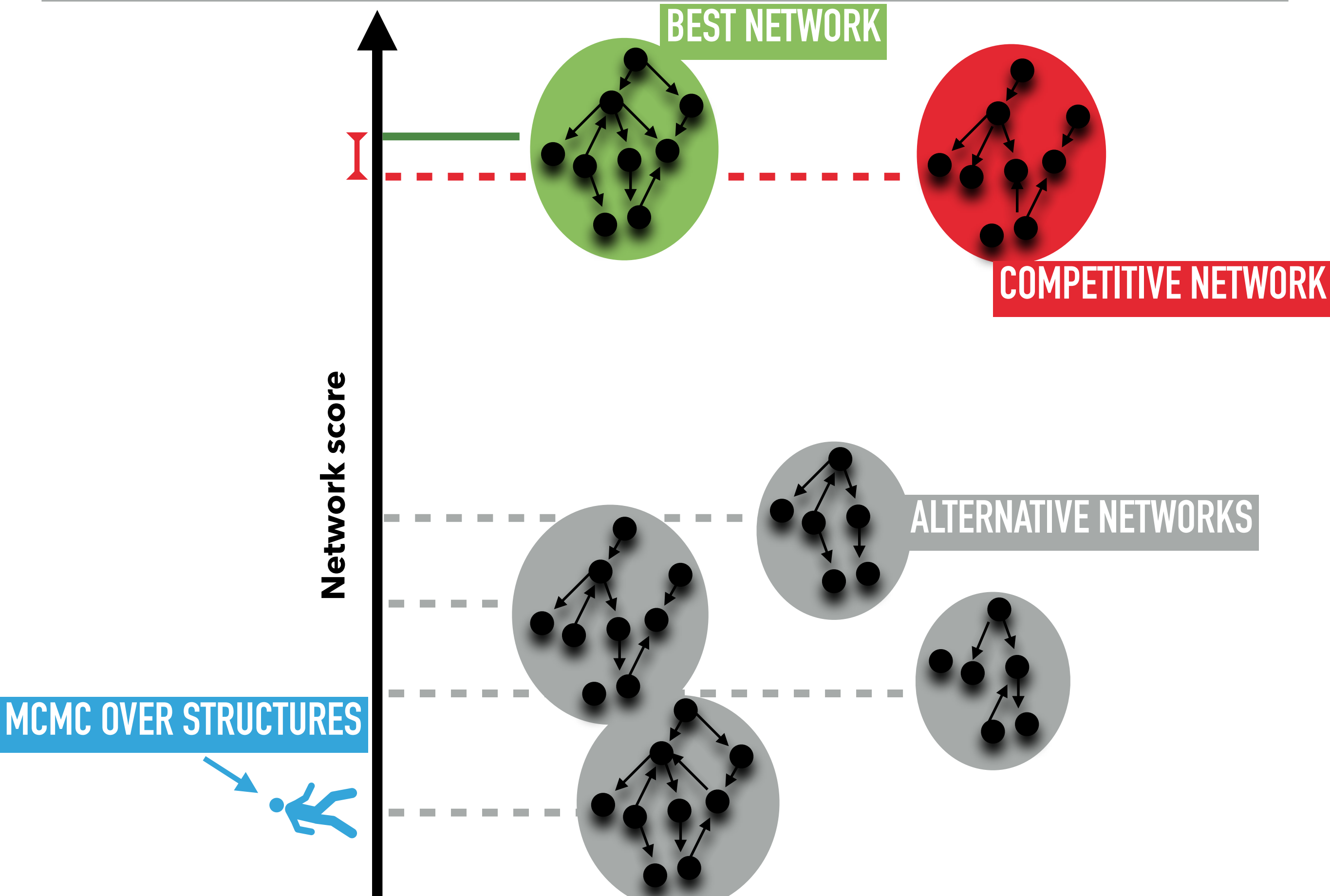
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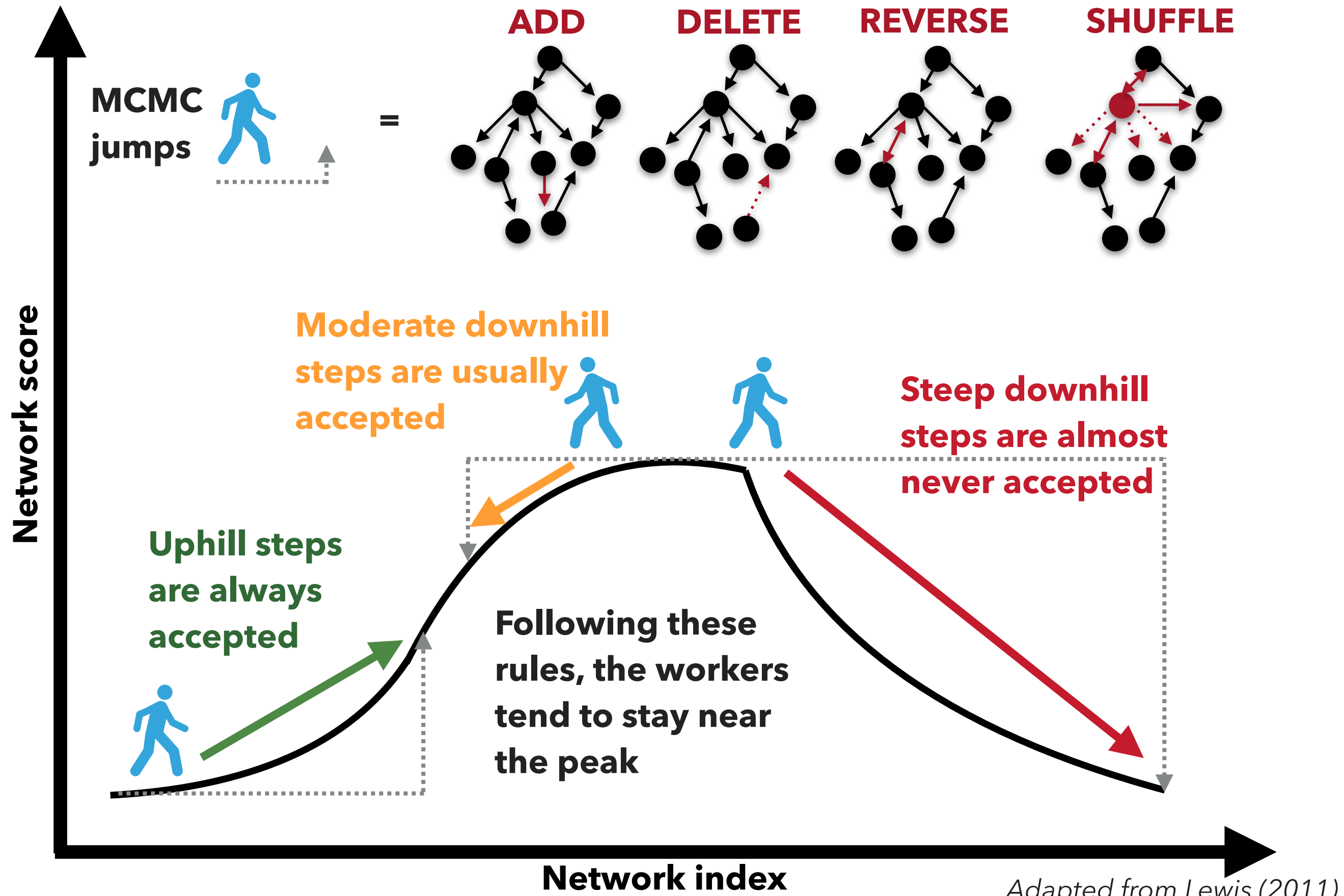




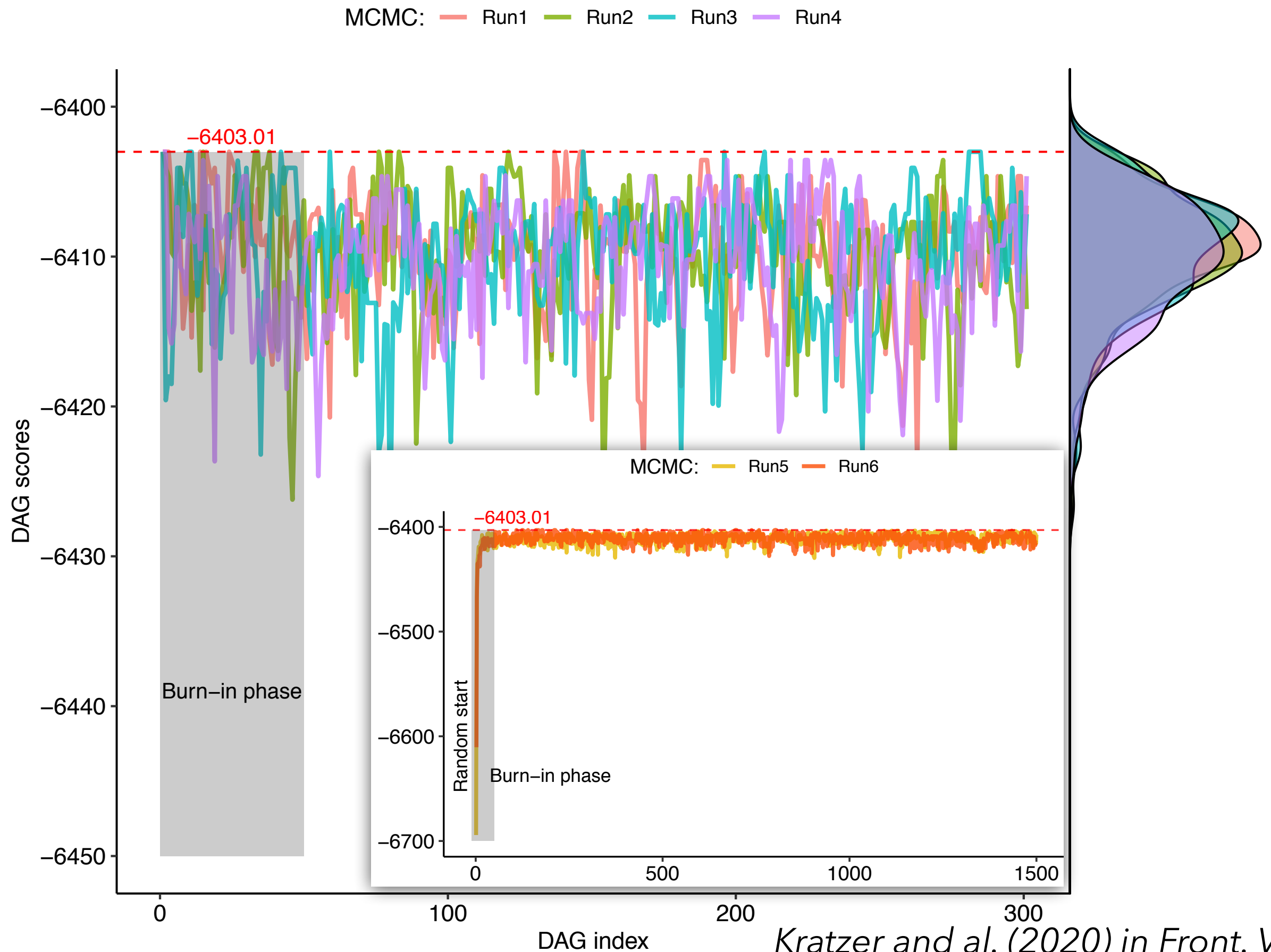
# MCMCABN - HOW TO CHOOSE THE BEST NETWORK?



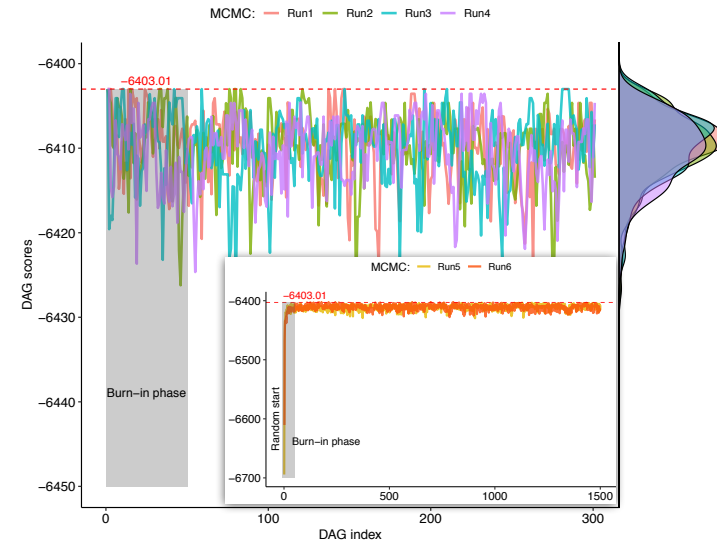
# MCMC TO COMPUTE THE POSTERIOR DISTRIBUTION OF NETWORK



# MCMC OVER STRUCTURE - POSTERIOR DISTRIBUTION

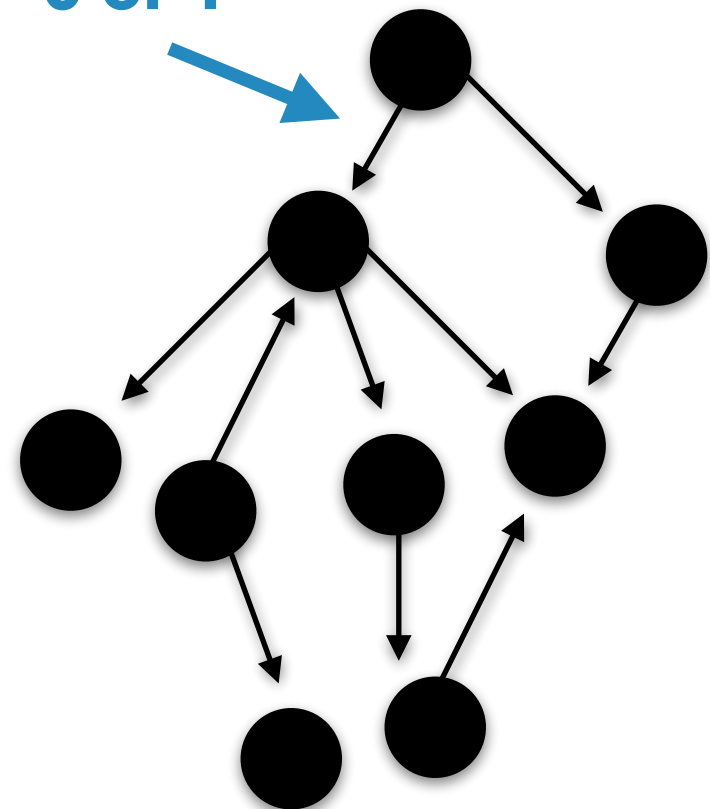


# WHY DO WE PERFORM MCMC OVER STRUCTURES?

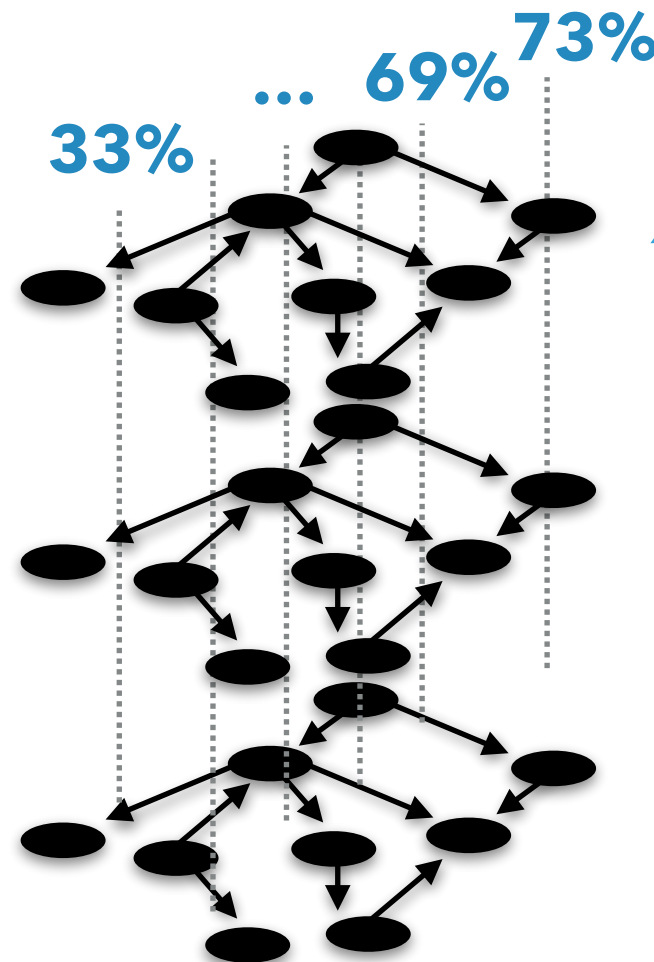


## Best Unique Bayesian Network

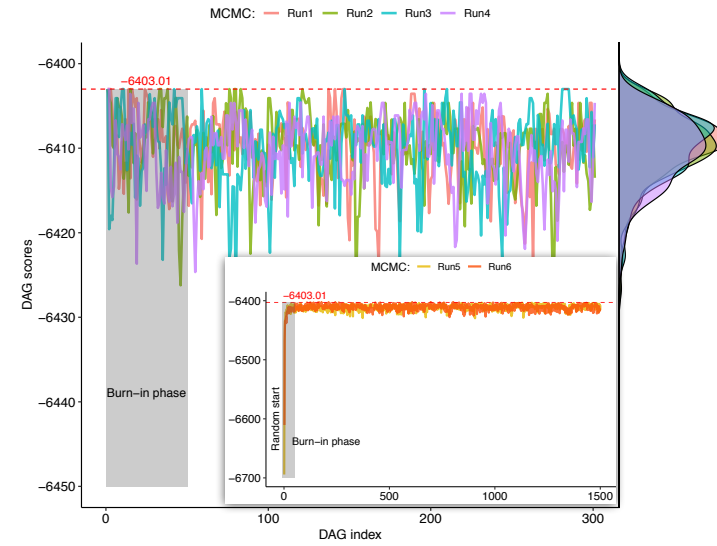
0 or 1



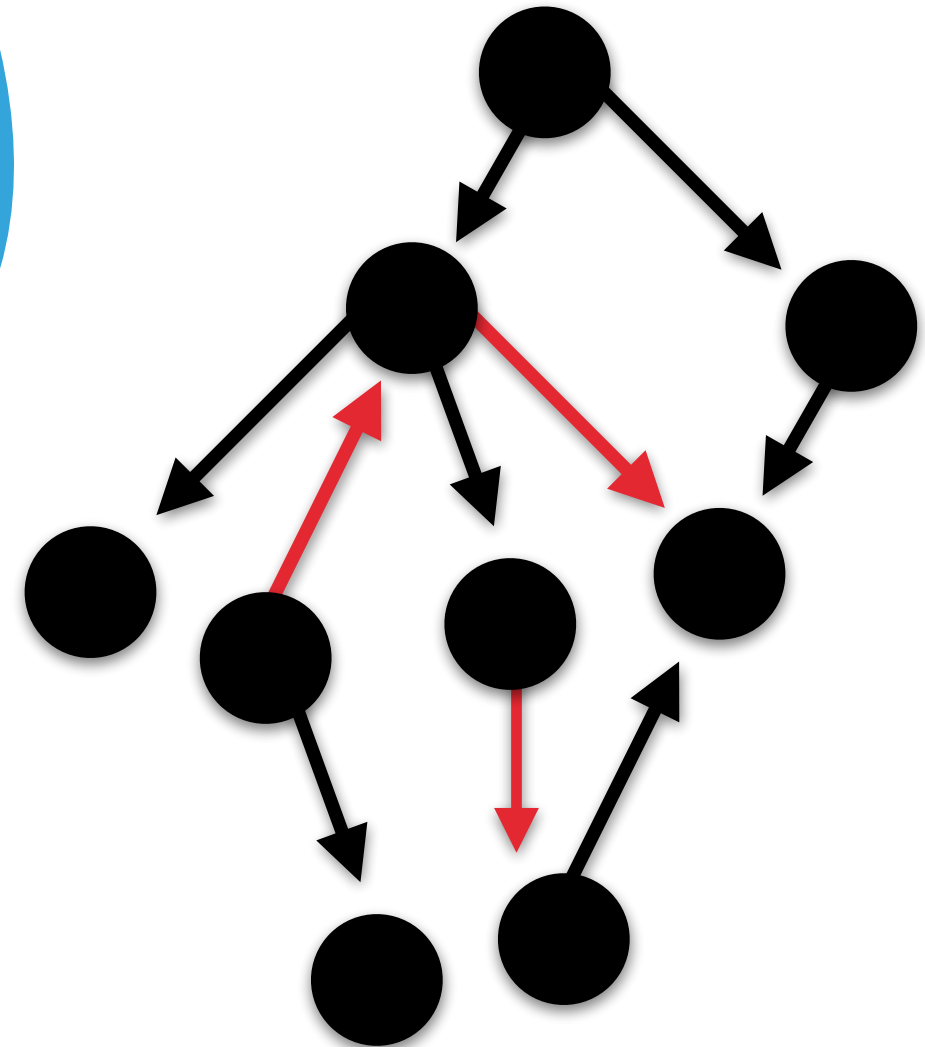
## Counting prevalence of each ARC



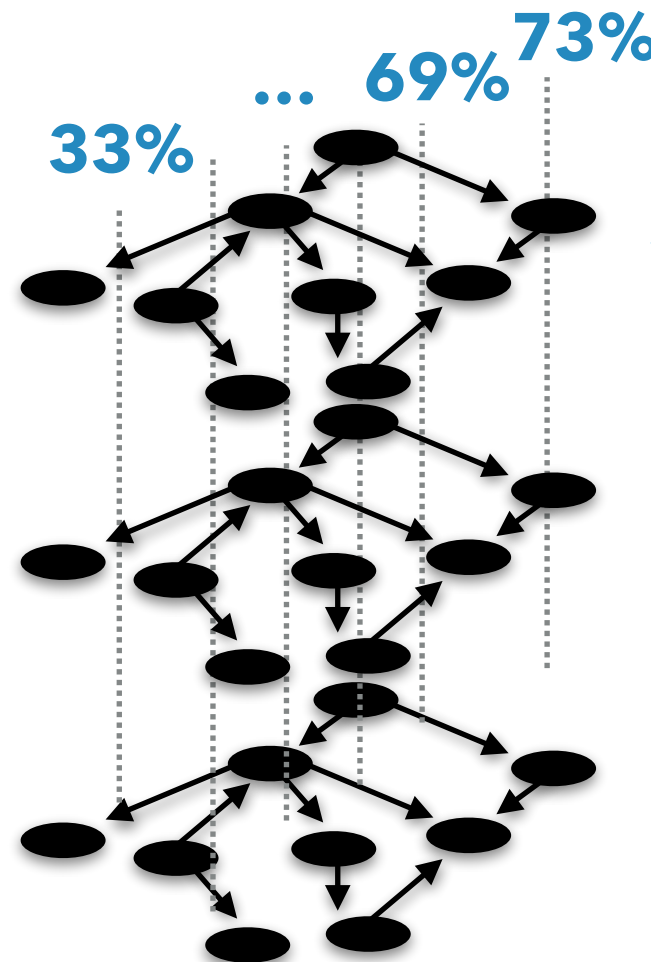
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## Structural queries

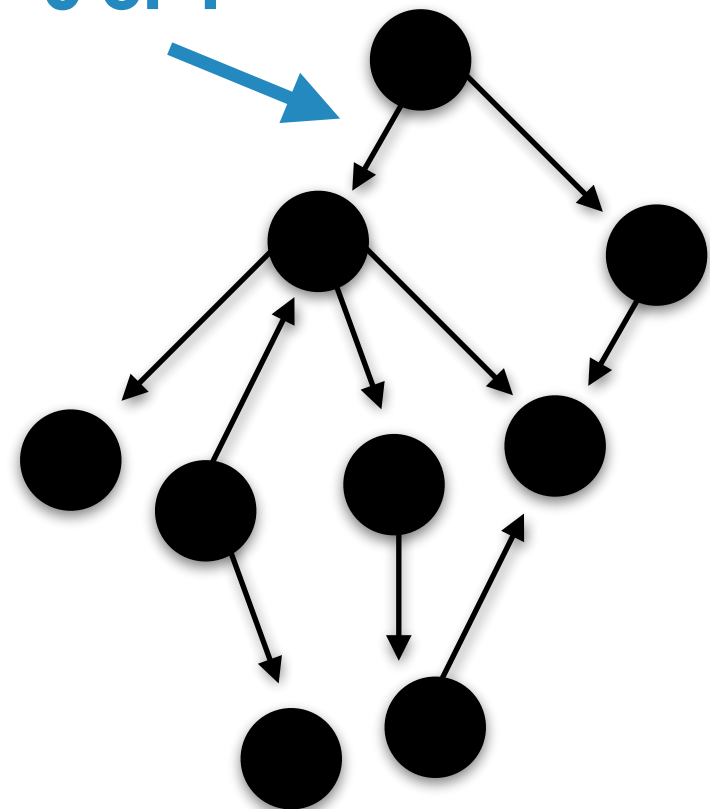


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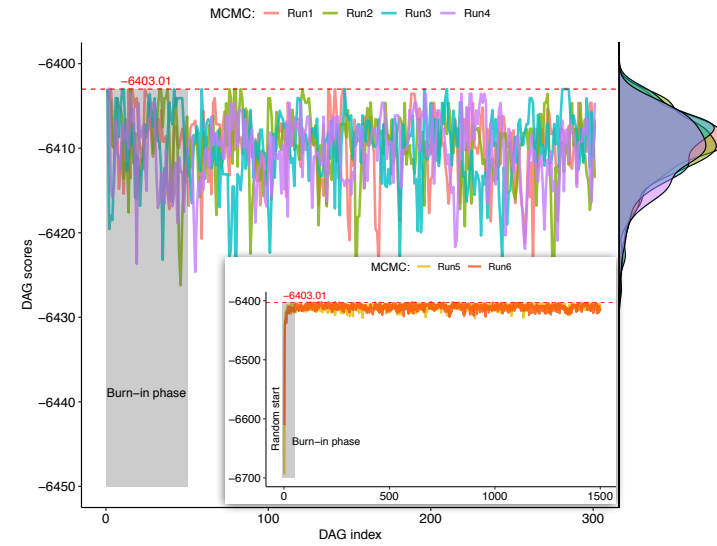
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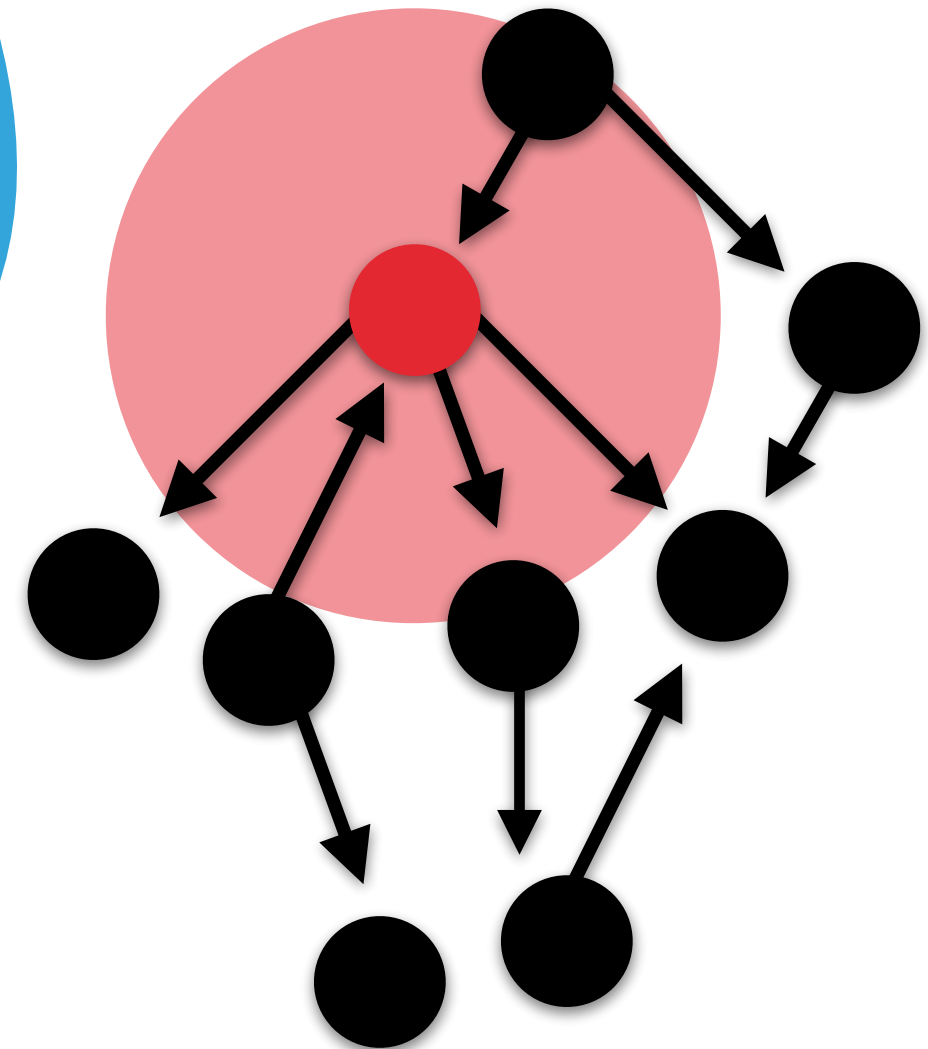




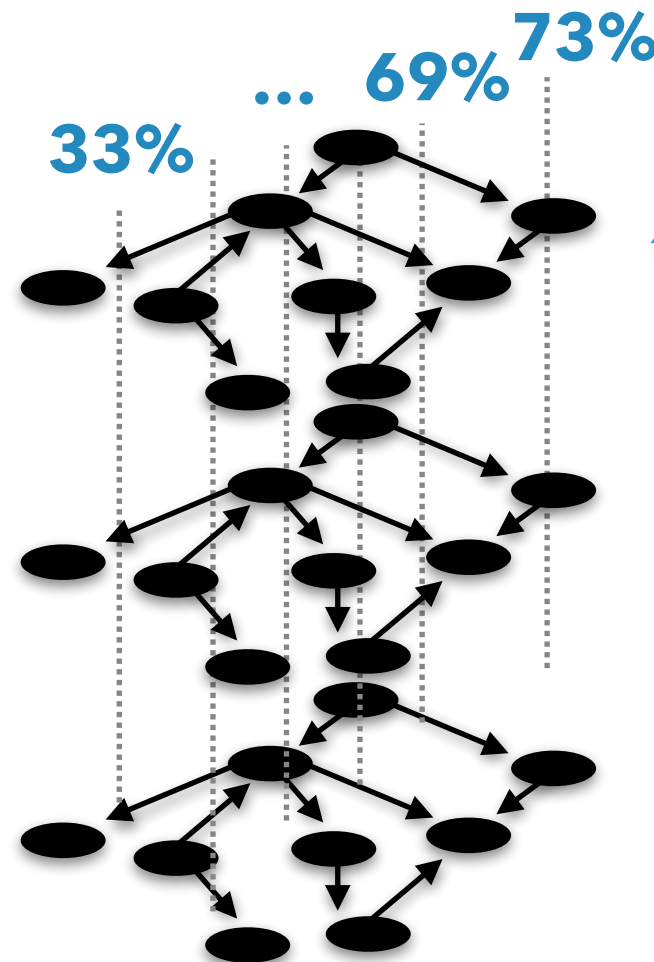
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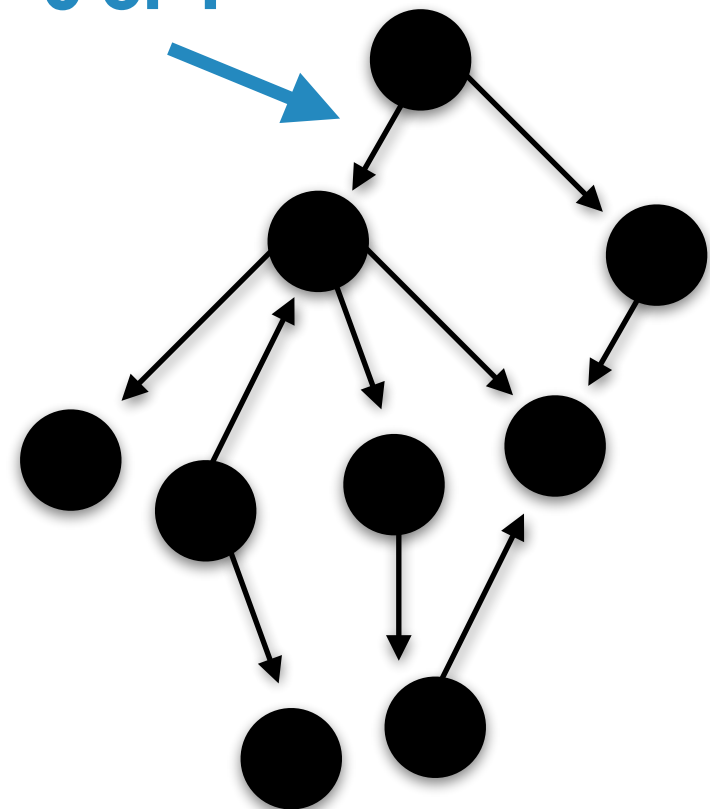


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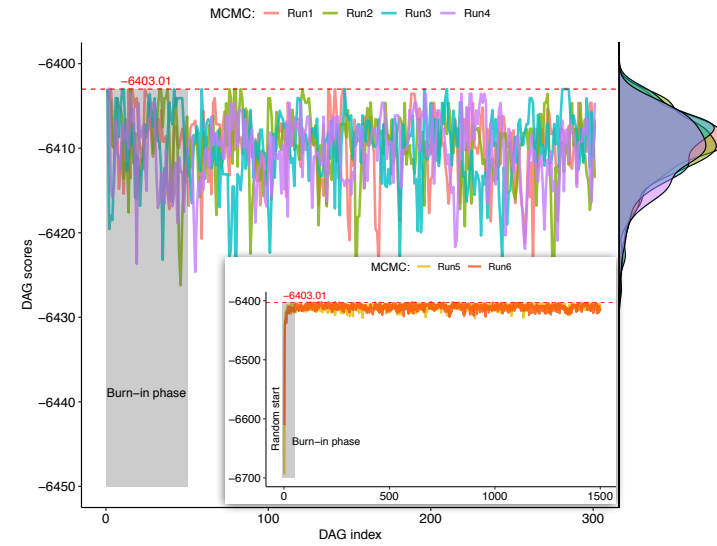
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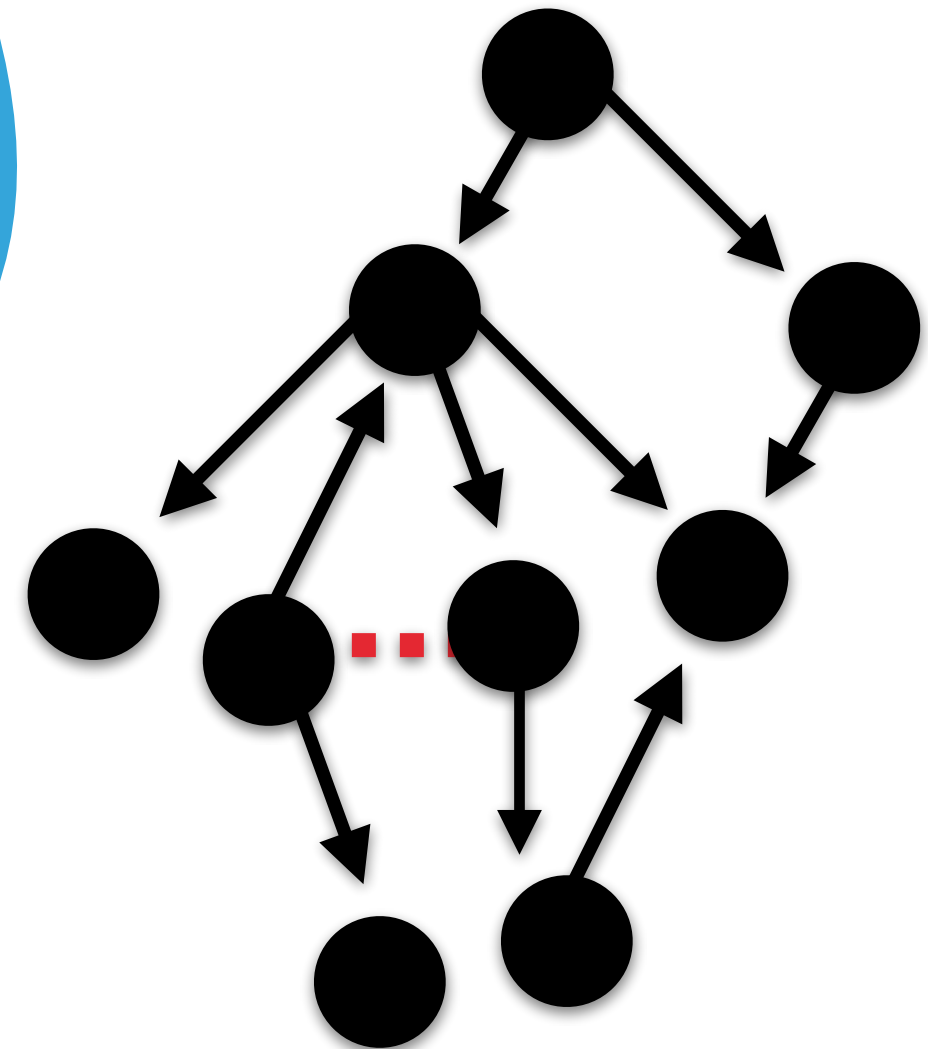




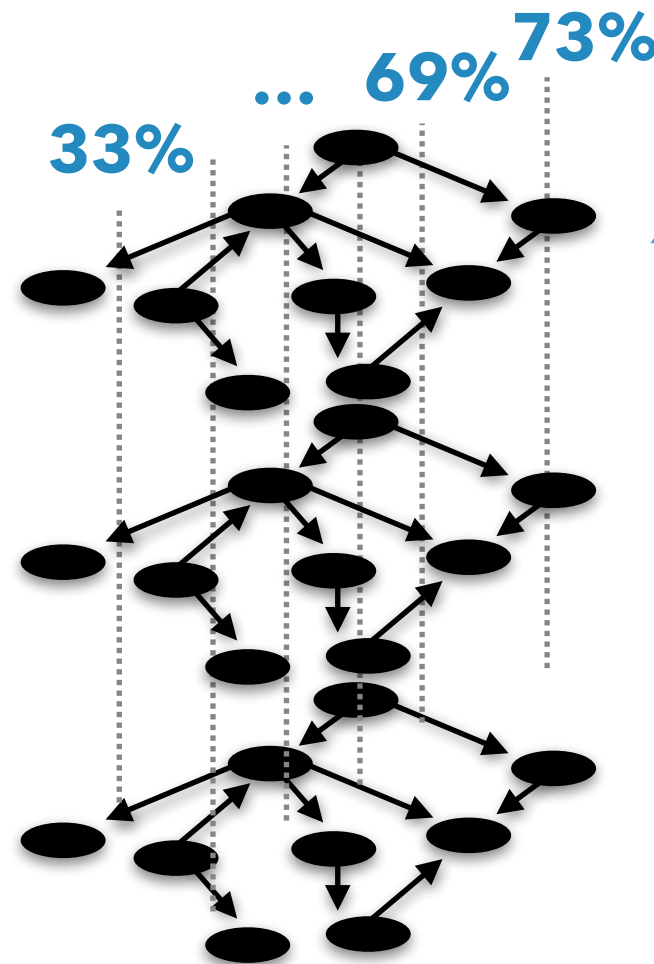
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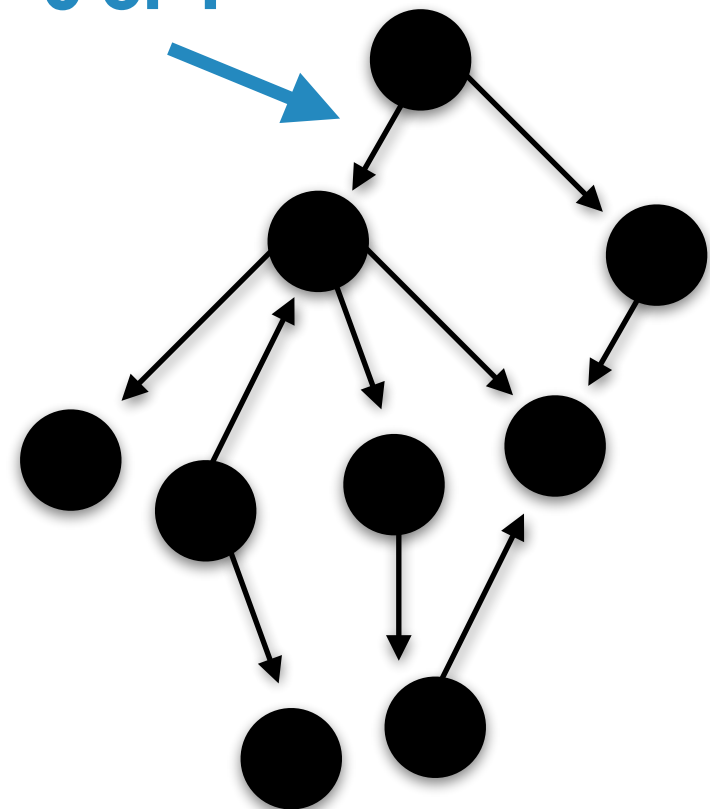


## Counting prevalence of each ARC



## Best Unique Bayesian Network

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# MCMC OVER STRUCTURES

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## *MCMC over structures*

- ▶ Selecting the most probable structure
- ▶ Controlling for overfitting
- ▶ Sampling the landscape of high scoring structures
  - ▶ In applied perspective avoid reducing the richness of BN modelling to only **one** structure
  - ▶ Quantify the marginal impact of relationships by marginalising out over structures

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# HANDS-ON EXERCICES