



**University of
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NATIONAL
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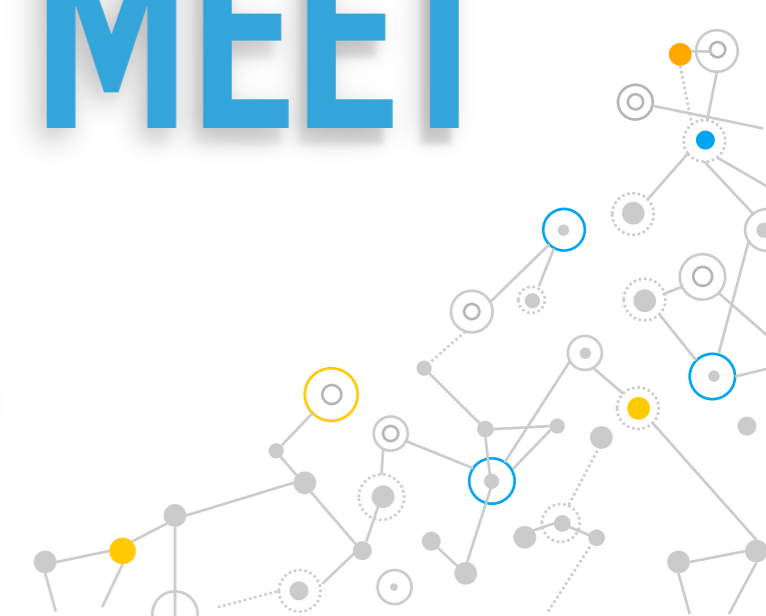
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SVEPM WORKSHOP, UTRECHT 27.03.2019

BAYESIAN NETWORKS MEET OBSERVATIONAL DATA



Credit Card Fraud Detection Using Bayesian and Neural Networks

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Abstract

This paper discusses automated credit card fraud detection by means of machine learning. In an era of digitalization, credit card fraud detection is of great importance to financial institutions. We apply two machine learning techniques suited for reasoning under uncertainty: artificial neural networks and

do the fraud detection. After a process of learning, the program is supposed to be able to correctly classify a transaction it has never seen before as fraudulent or not fraudulent, given some features of that transaction.

The structure of this paper is as follows: first we introduce the reader to the domain of credit card fraud detection. In Sections 3 and 4 we briefly ex-

MOTIVATIONAL EXAMPLE: CREDIT CARD FRAUD DETECTION PREDICTION

Credit Card Fraud Detection Using Bayesian and Neural Networks

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experiment	$\pm 10\%$ false pos	$\pm 15\%$ false pos
ANN-fig 2(a)	60% true pos	70% true pos
ANN-fig 2(a)	47% true pos	58% true pos
ANN-fig 2(c)	60% true pos	70% true pos
BBN-fig 2(e)	68% true pos	74% true pos
BBN-fig 2(g)	68% true pos	74% true pos

Abstract

This paper discusses credit card fraud detection by means of machine learning. In the era of digitalization, credit card fraud has become of great importance to financial institutions. We compare two machine learning techniques suited for reasoning under uncertainty: artificial neural networks and

Table 1: This table compares the results achieved with ANN and BBN, for a false positive rate of respectively 10% and 15%.

process of learning, we aim to correctly classify transactions before as fraudulent. The features of that process are as follows: first we introduce the reader to the domain of credit card fraud detection. In Sections 3 and 4 we briefly ex-

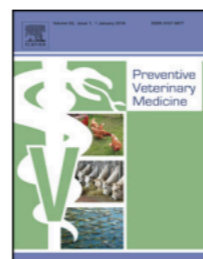
MOTIVATIONAL EXAMPLE: VETERINARY EPIDEMIOLOGY DATA VISUALISATION



Contents lists available at SciVerse ScienceDirect

Preventive Veterinary Medicine

journal homepage: www.elsevier.com/locate/prevetmed



Using Bayesian networks to explore the role of weather as a potential determinant of disease in pigs

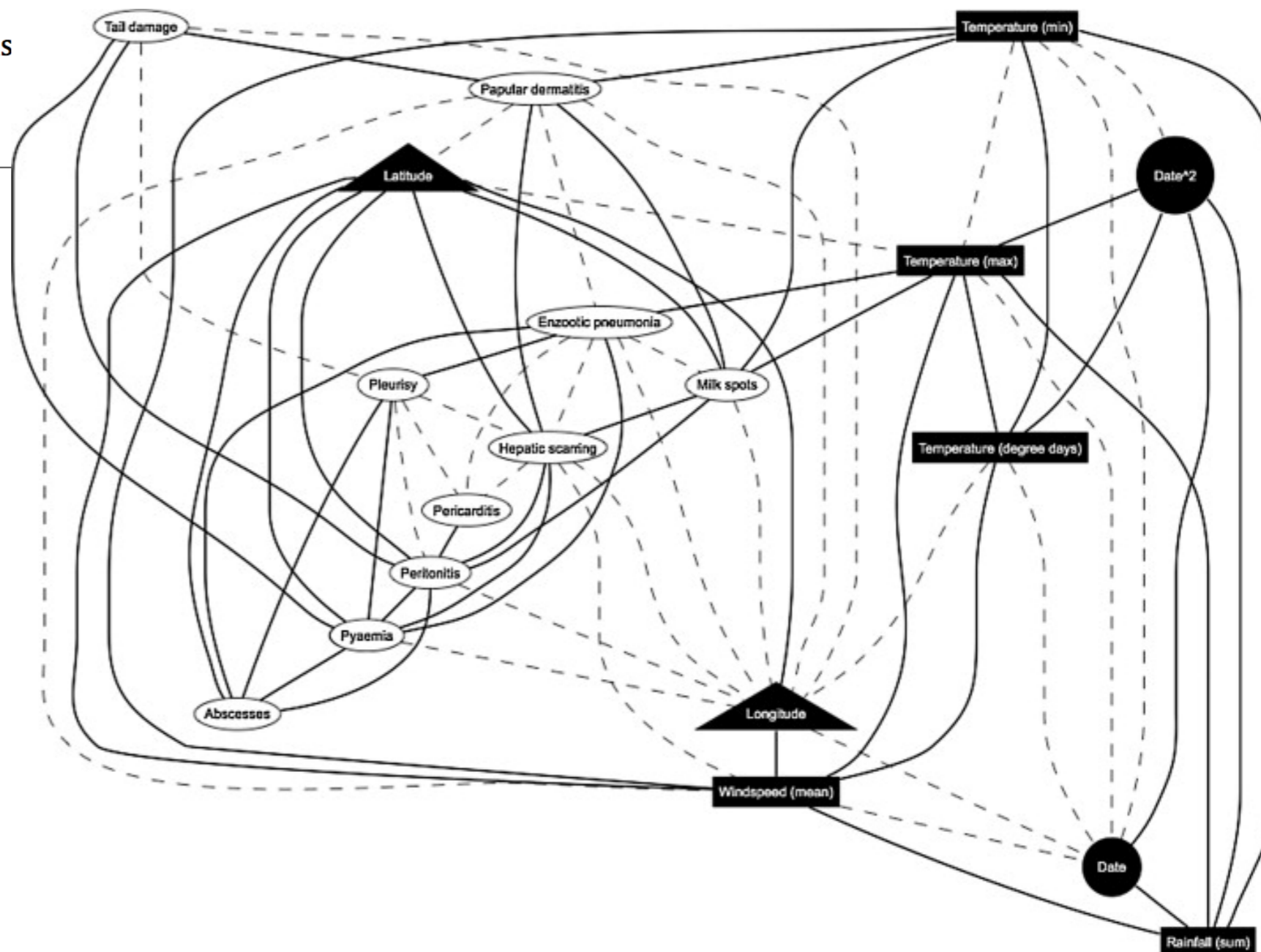


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MOTIVATIONAL EXAMPLE: SOCIAL SCIENCES

DATA INTERPRETATION

Discovering complex interrelationships between socioeconomic status and health in Europe: A case study applying Bayesian Networks

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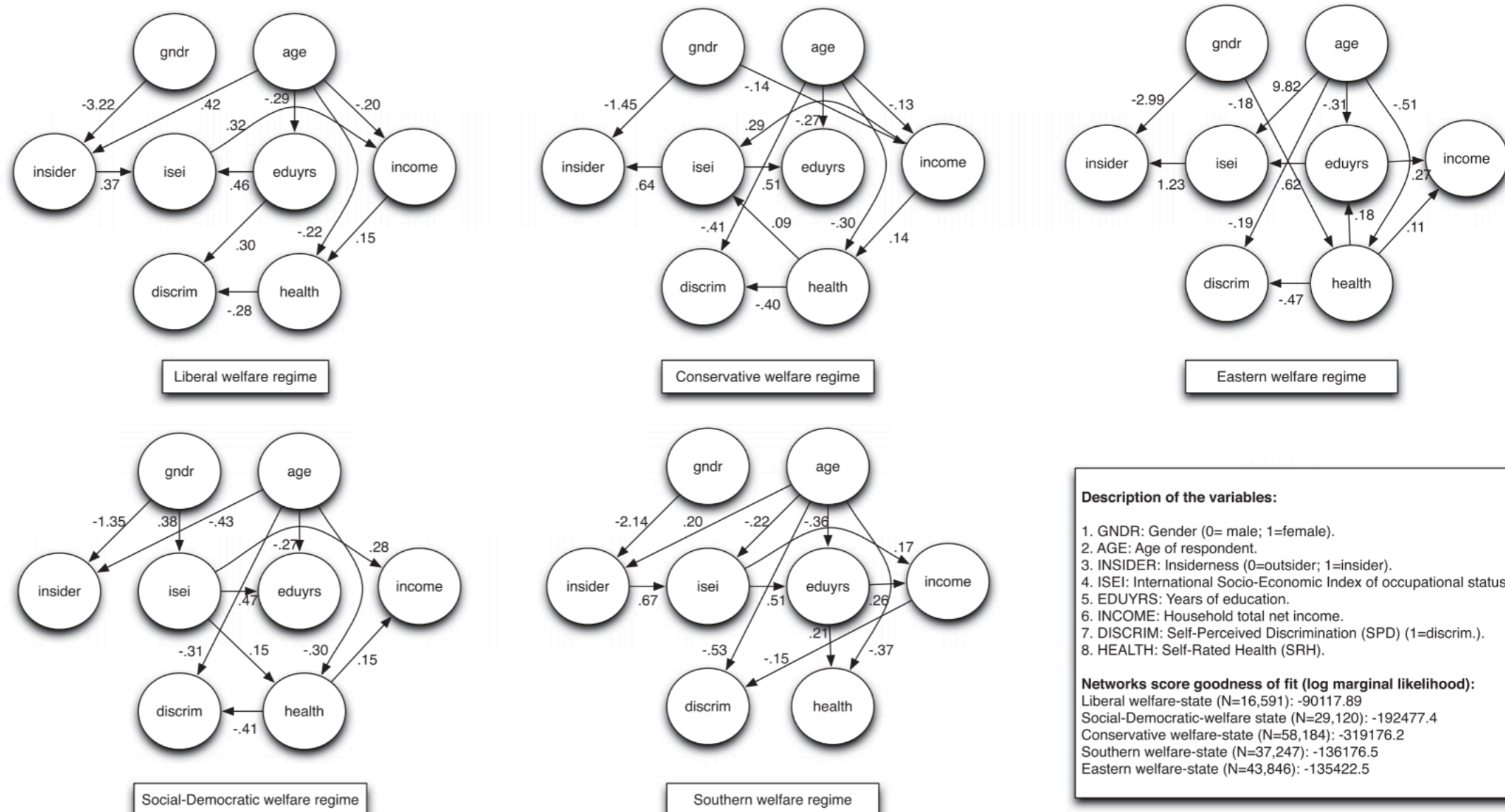


Fig. 1. Bayesian networks describing interrelationships between SES and health in five European welfare states.

BAYESIAN NETWORKS IN THE MACHINE LEARNING WORLD

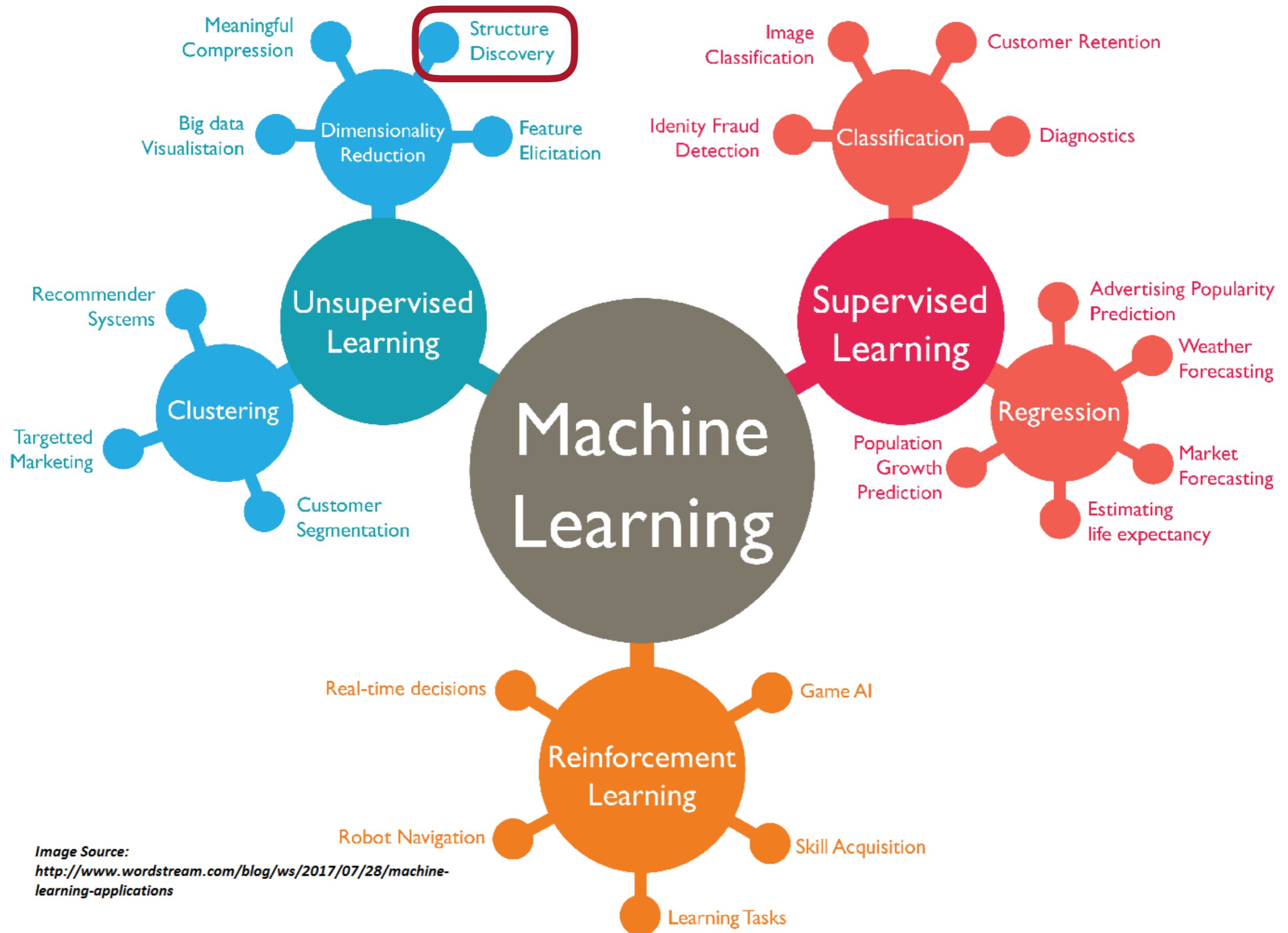


Image Source:
<http://www.wordstream.com/blog/ws/2017/07/28/machine-learning-applications>

OUTLINE OF THE TALK

Objective of the workshop:

How to **learn Bayesian networks** from observational data?

OUTLINE OF THE TALK

Objectif of the workshop:

select

How to ~~learn~~ Bayesian networks from observational data?

Bayesian Networks are defined by two elements:

Network structure:

Directed Acyclic Graph (**DAG**): $G = (V, A)$

in which each node $v_i \in V$ corresponds to a random variable X_i

Probability distribution:

Probability distribution X with parameters Θ , which can be factorised into smaller local probability distributions according to the arcs $a_{ij} \in A$ present in the graph.

A BN encodes the factorisation of the joint distribution

$$P(\mathbf{X}) = \prod_{j=1}^n P(X_j \mid \mathbf{Pa}_j, \Theta_j), \text{ where } \mathbf{Pa}_j \text{ is the set of parents of } X_j$$

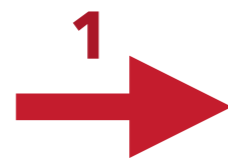
PLAN

1. From observational dataset deduce probabilistic model
 - Usually discrete BN or jointly Gaussian
 - Epidemiological constrain: mixture of distributions
2. From probabilistic model deduce structure

EXPONENTIAL FAMILY

Observational dataset

X1	X2	X3	...
12	23	53	...
32	31	23	...
10	16	45	...
...

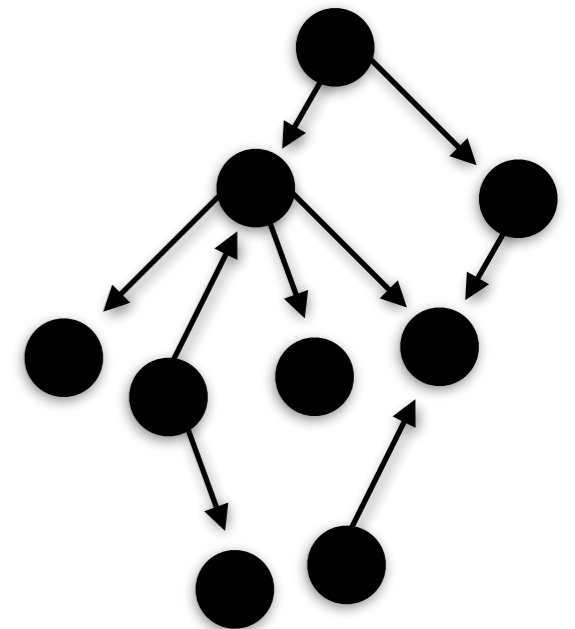


Probabilistic model


$$P(X_1, \dots, X_n) = P(X_i | X_j, \dots) \dots$$



Network structure



COMBINATORIAL WALL

# Nodes	# DAGs	Inference	Typical domain of interest
1 - 15 Nodes	$< 10^{41}$ DAGs	Exact inference	
16 - 25 Nodes	$< 10^{100}$ DAGs	Exact inference possible	
26 - 50 Nodes	$< 10^{400}$ DAGs	Approximate inference	
51 - 100 Nodes	$< 10^{1700}$ DAGs	Approximate inference	
101 - 1000 Nodes	$< 10^{100000}$ DAGs	(very) approximative inference	

Approximations:

- ▶ limiting number of parents per node
- ▶ Decomposable scores/efficient algorithm
- ▶ Score equivalence

SOME ELEMENTS OF PROBABILITY THEORY

The **conditional probability** of A given B is: $P(A | B) = \frac{P(A, B)}{P(B)}$

Bayes theorem: $P(A | B) = \frac{P(B | A)P(A)}{P(B)}$

Let A, B and C non intersecting subsets of nodes in a DAG G

A is **conditionally independent** of B given C if: $A \perp\!\!\!\perp_P B | C$

$$P(A, B | C) = P(A | C)P(B | C)$$

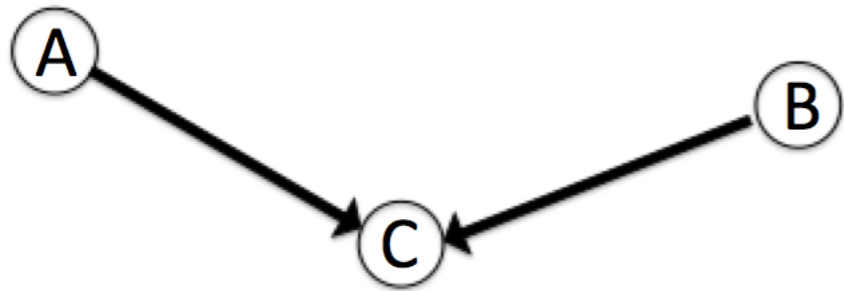
ELEMENT OF GRAPH THEORY

Let A , B and C non intersecting subsets of nodes in a DAG G

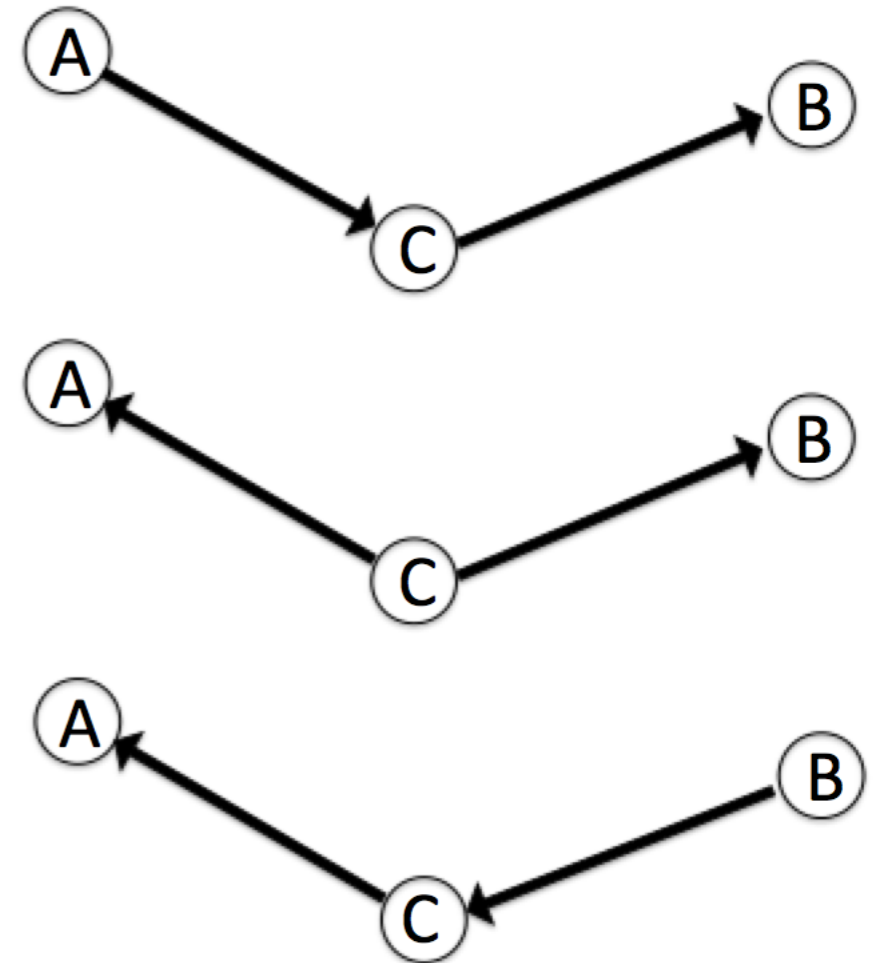
A is **conditionally independent** of B given C if: $A \perp_P B | C$

$$P(A, B | C) = P(A | C)P(B | C)$$

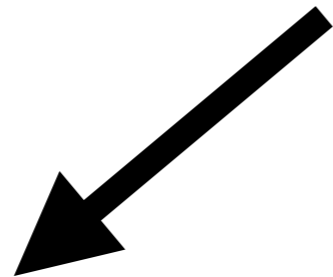
$A \not\perp_P B | C$



$A \perp_P B | C$

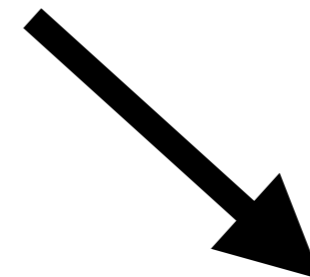


$$\mathcal{M} = (\mathcal{S}, \Theta_{\mathcal{M}})$$



Model selection

Structure learning

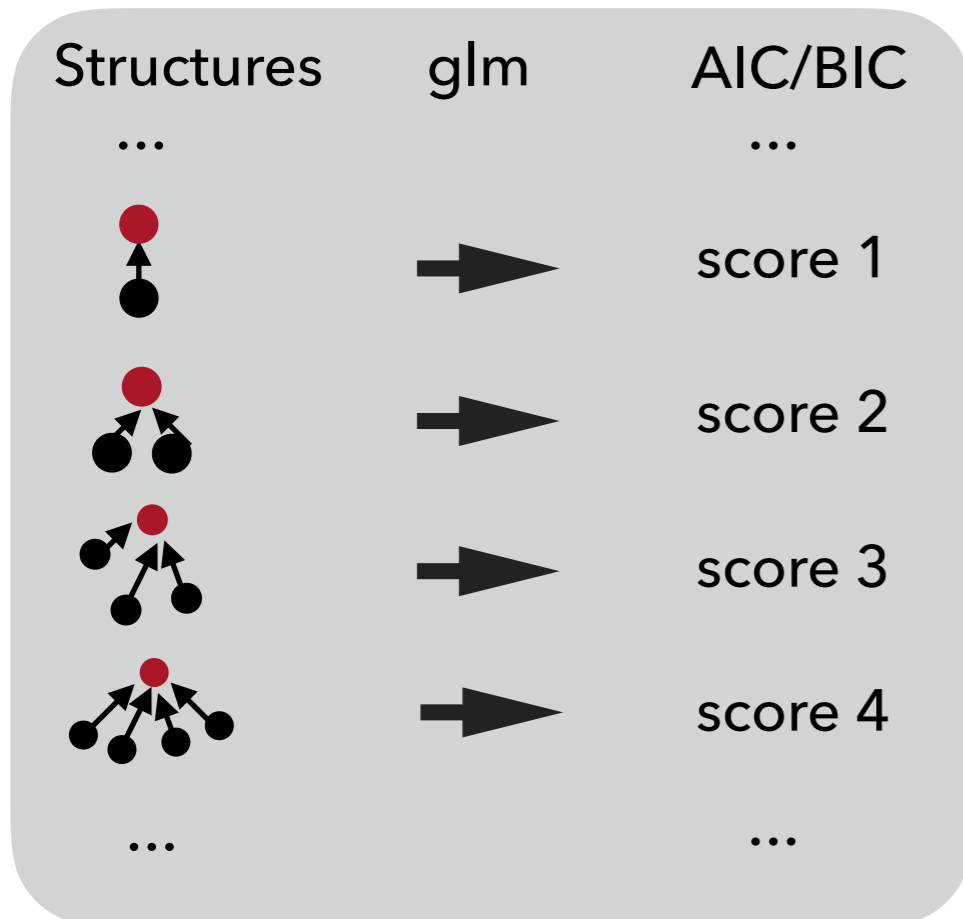


Parameter estimation

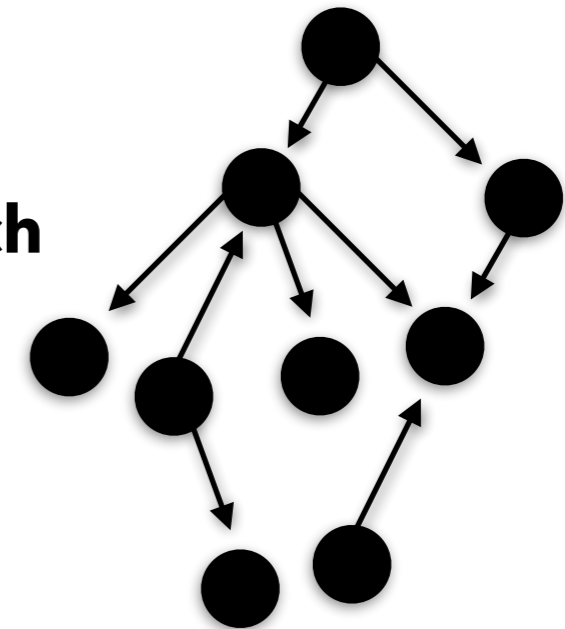
Parameter learning

$$P(\mathcal{M}|\mathcal{D}) = \underbrace{P(\Theta_{\mathcal{M}}, \mathcal{S}|\mathcal{D})}_{\text{model learning}} = \underbrace{P(\Theta_{\mathcal{M}}|\mathcal{S}, \mathcal{D})}_{\text{parameter learning}} \cdot \underbrace{P(\mathcal{S}|\mathcal{D})}_{\text{structure learning}}$$

Search and score algorithm

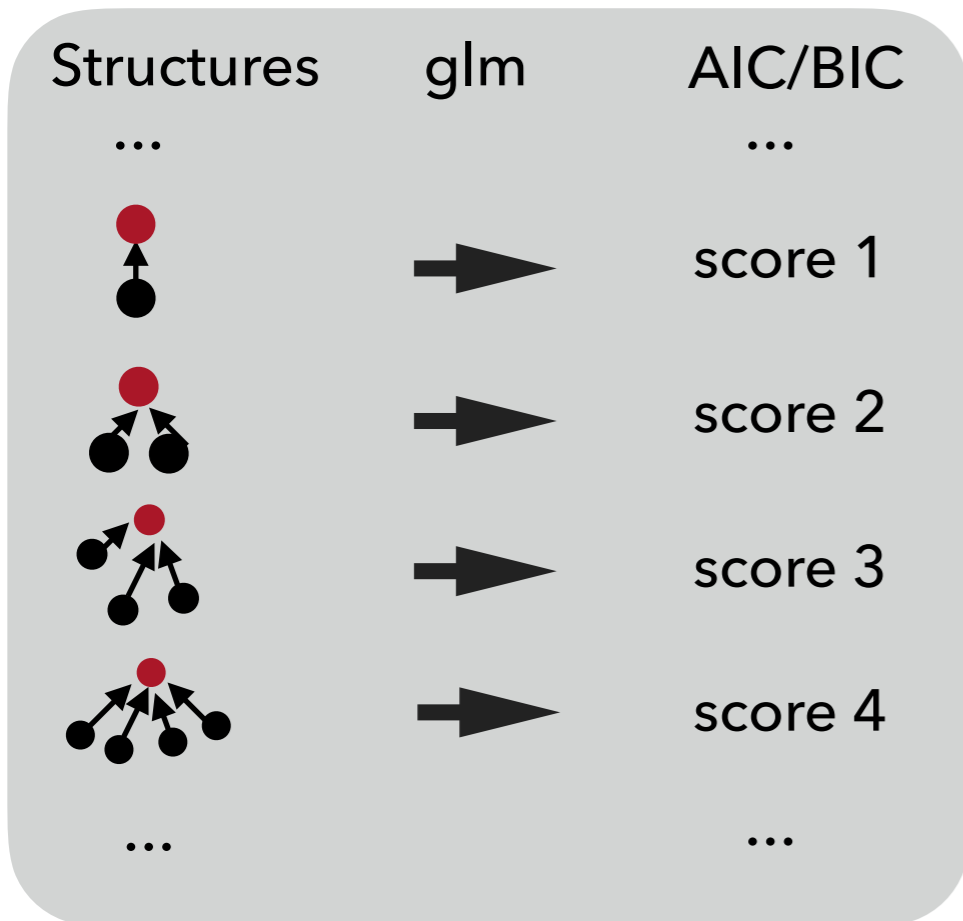


Exact or heuristic search

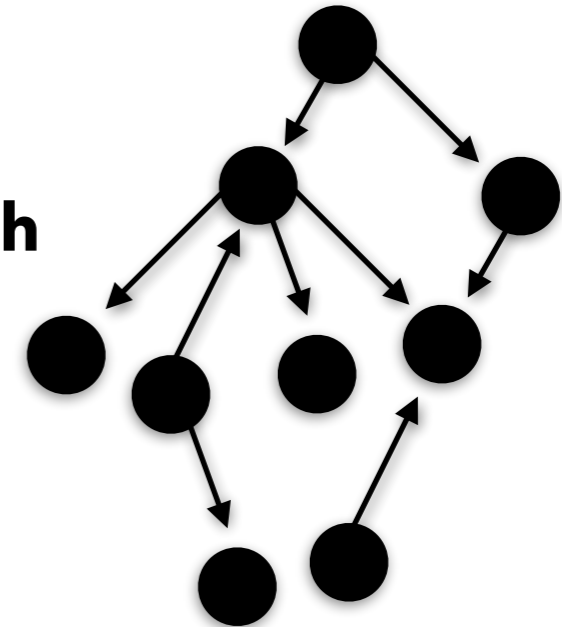


Bayesian network with highest posterior probability

Search and score algorithm



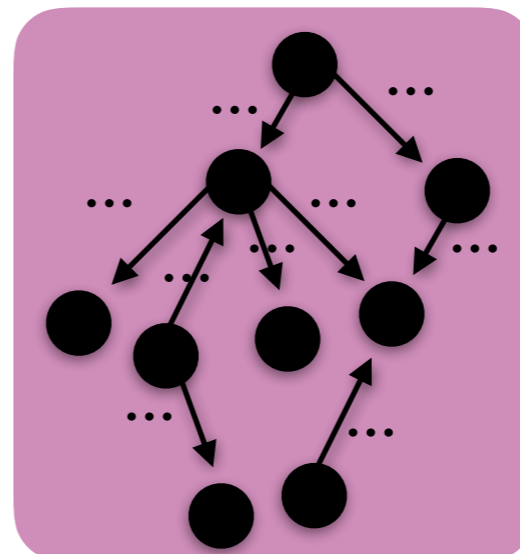
Exact or heuristic search



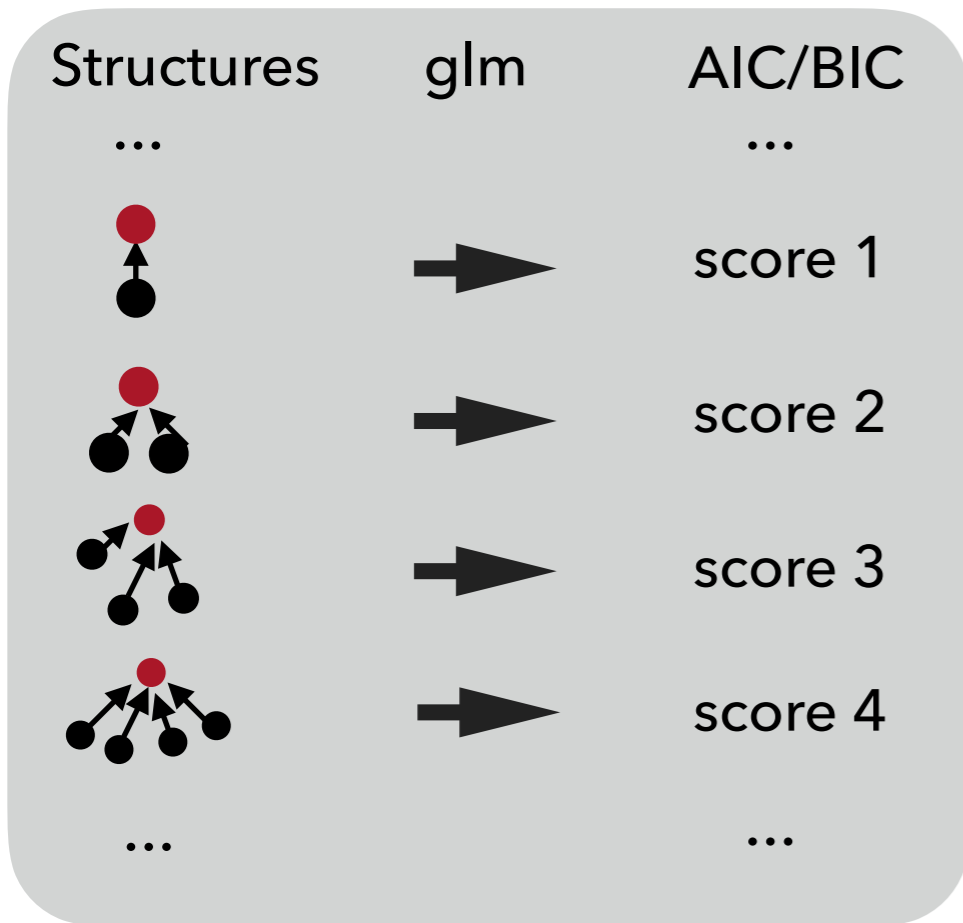
Bayesian network with highest posterior probability

Parameter estimation

- ▶ compute marginal posterior density
- ▶ regression estimate



Search and score algorithm

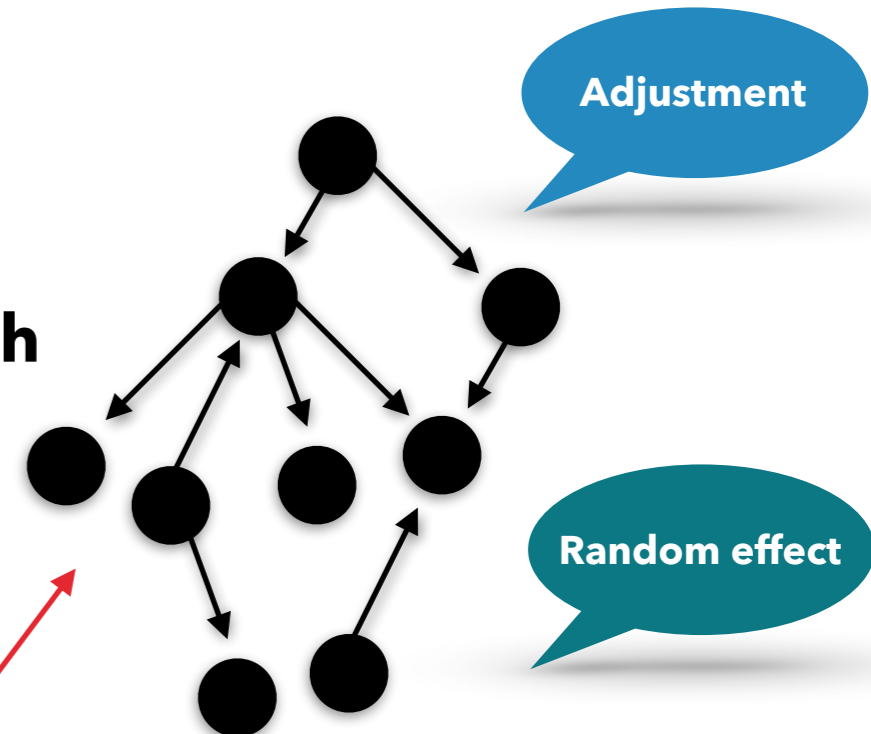


Exact or heuristic search



Causality!

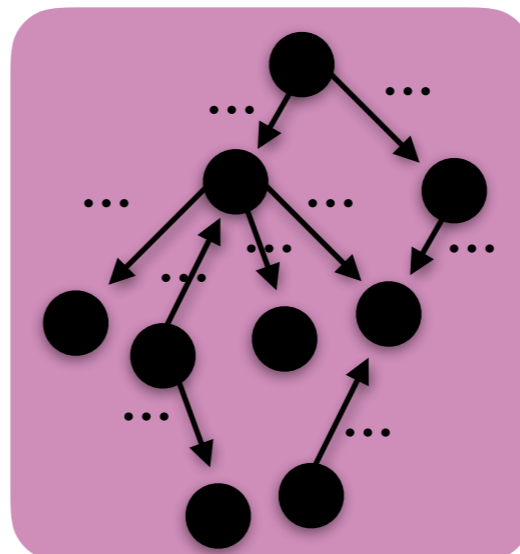
Ban/Retain structures



Bayesian network with highest posterior probability

Parameter estimation

- ▶ compute marginal posterior density
- ▶ regression estimate



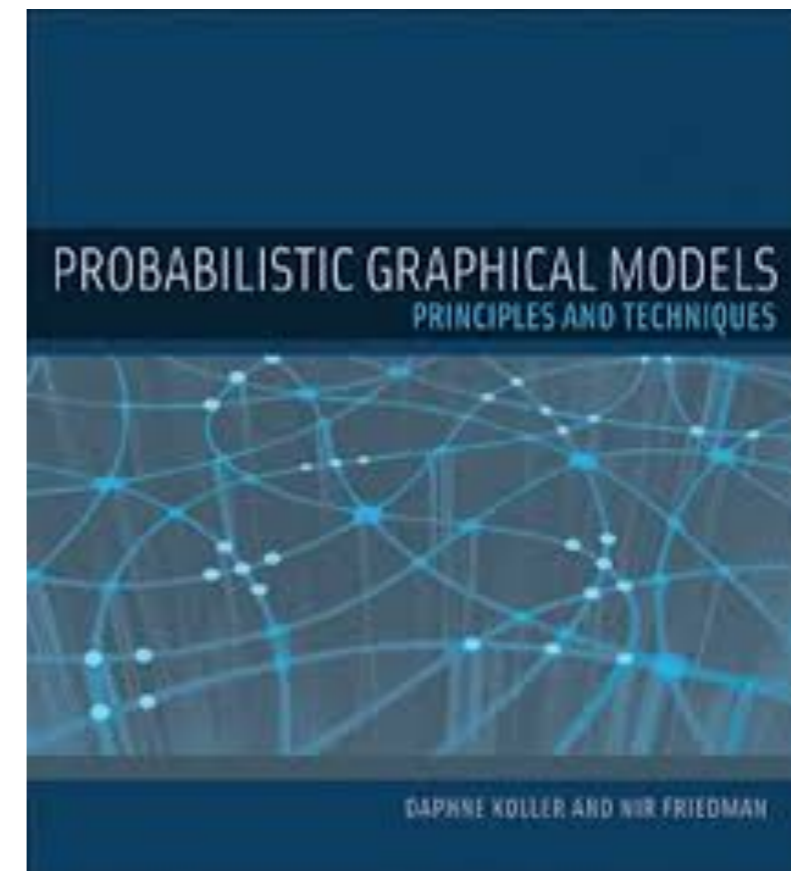
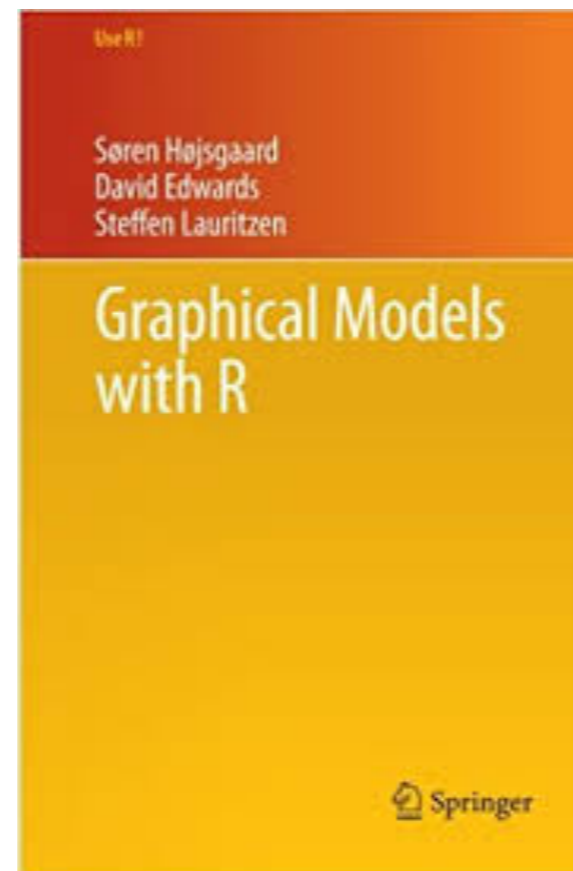
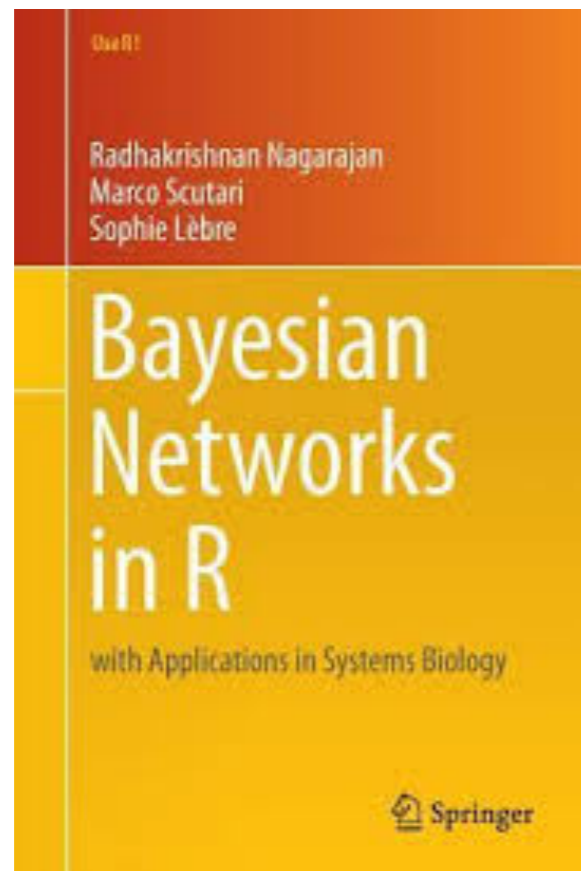
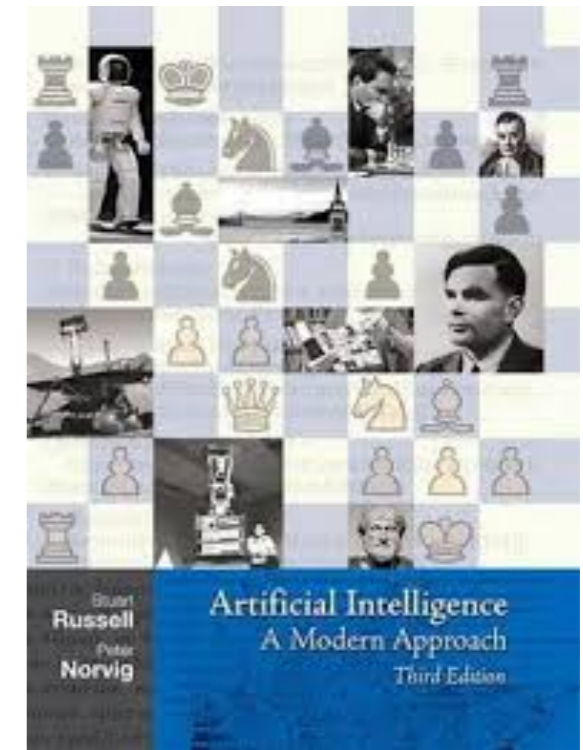
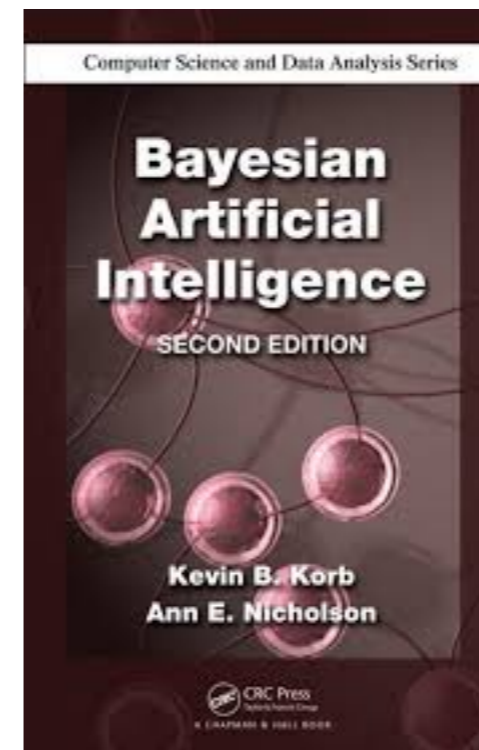
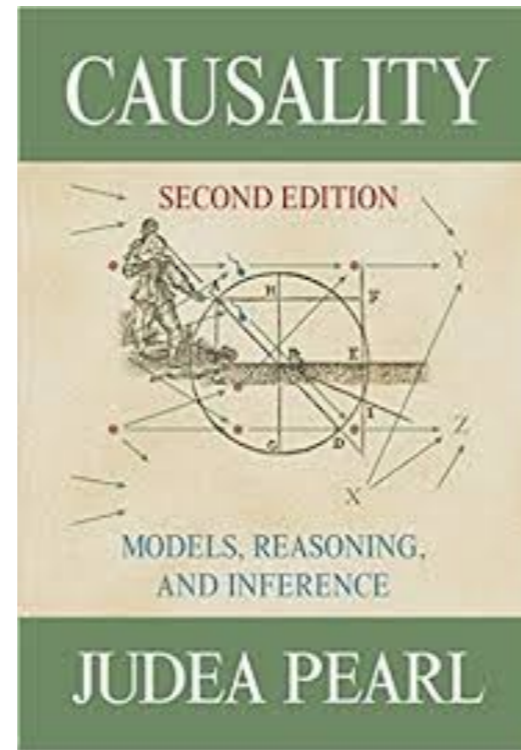
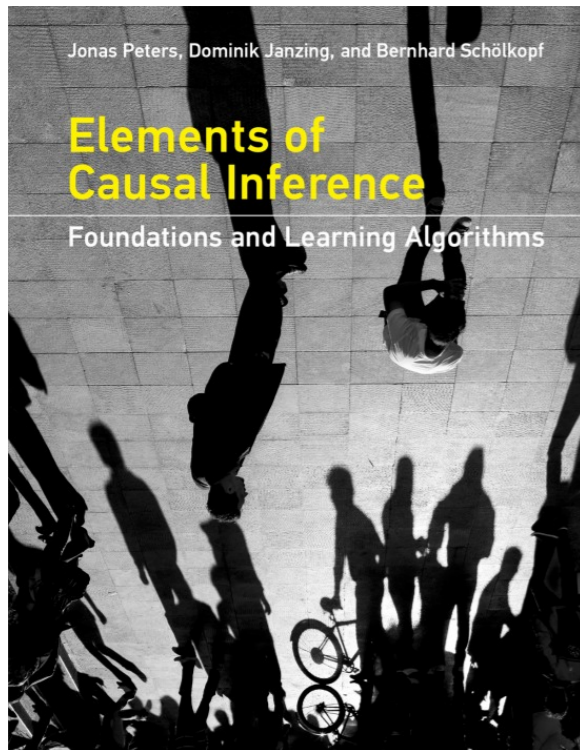
Using R

`buildscorecache()`

`mostprobable()`

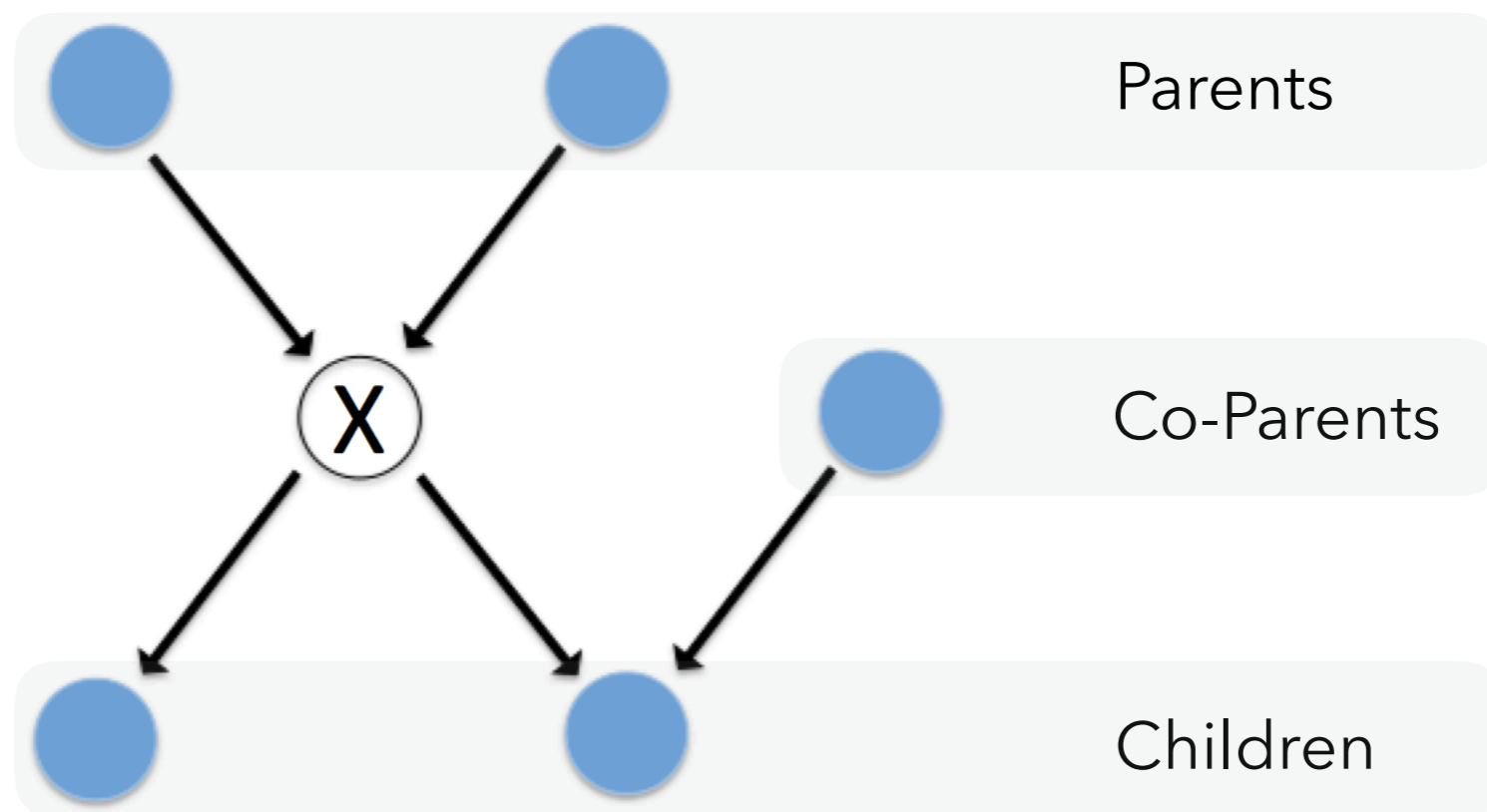
`fitabn()`

SELECTED BIBLIOGRAPHY



ELEMENT OF GRAPH THEORY: MARKOV BLANKET

The **Markov Blanket** of a node is the set of **parents**, **co-parents** and **children**.



$$P(X_k | X_n, k \neq n) = P(X_k | X_{\text{MB}(k)}), \forall k$$

The **Markov Blanket** of a node is the set of nodes that **shields** the index node from the rest of the network

Local Markov property:

$$X \perp \text{Non-Descendants}(X) | Pa(X)$$

LEARNING BAYESIAN NETWORKS

- ▶ In a practical perspective, for **observational** data, if learning algorithms rely on **probabilistic learning algorithm**. Then one can learn up to the **Markov equivalence class**.
- ▶ **Markov equivalence class** are the set of DAGs that have the same **skeleton** and **v-structure**.

